

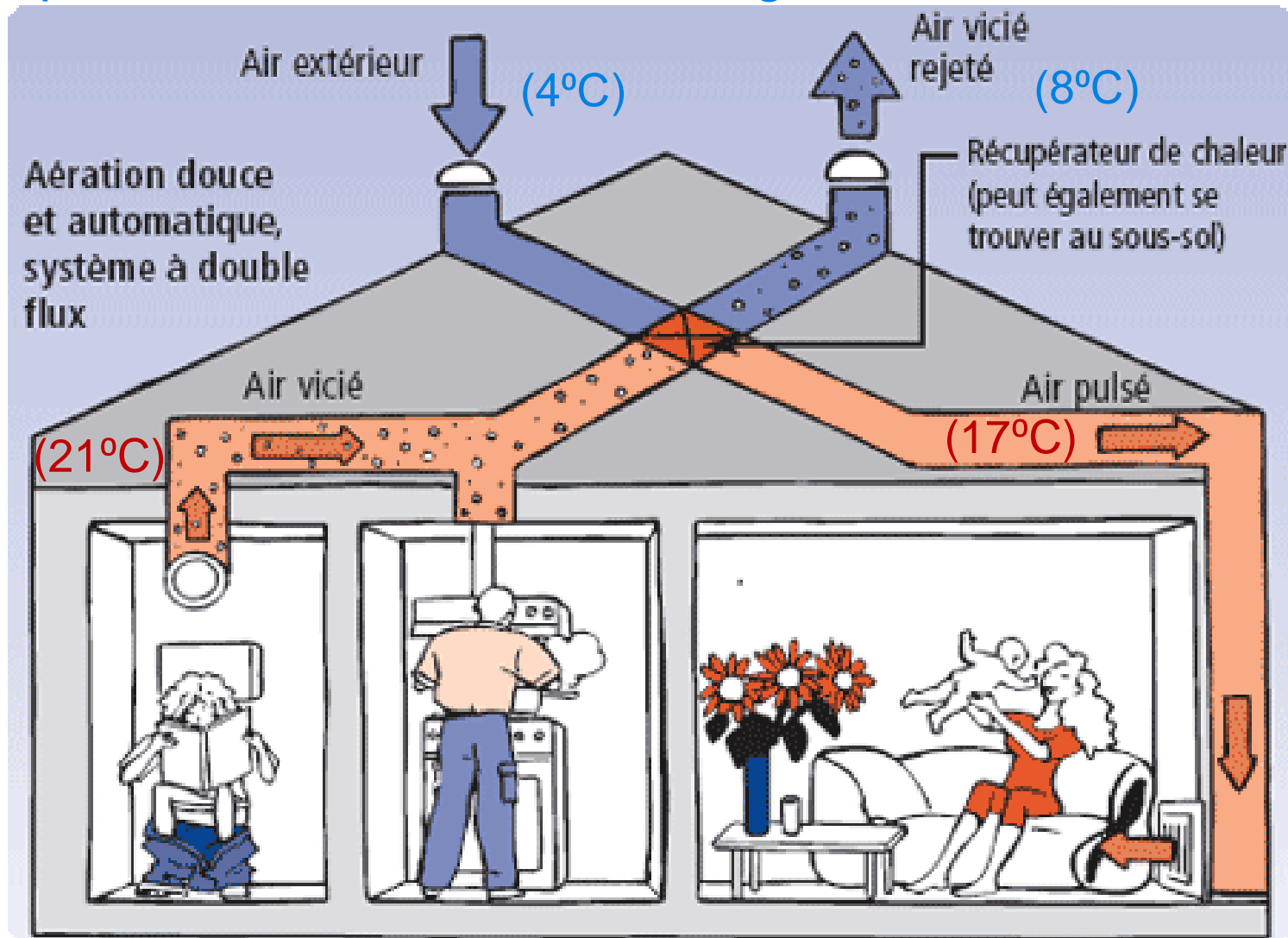
Pinch Analysis for Heat Integration

Martin Patel
Mostafa Babaei
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Heat recovery: Space heating

Récupération de chaleur - Chauffage des locaux



Double flux avec récupération de chaleur

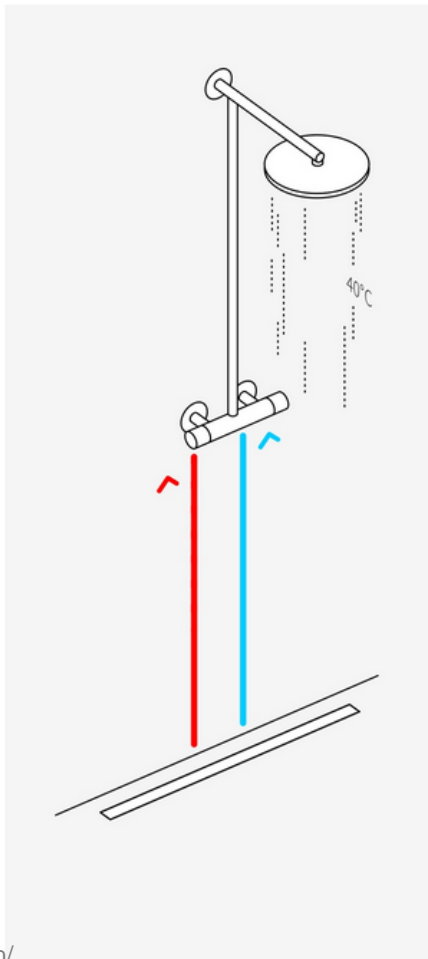
Komfortlüftung mit Wärmerückgewinnung

Heat recovery – Joulia shower

Récupération de chaleur - Douche Joulia

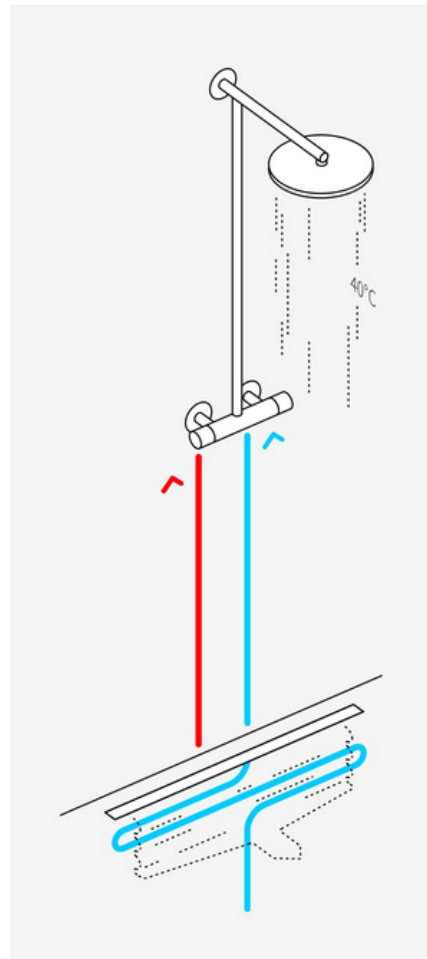
Before:

The cold and warm water is directly connected to the mixing valve. The used warm shower water regrettably flows into the sewerage system.



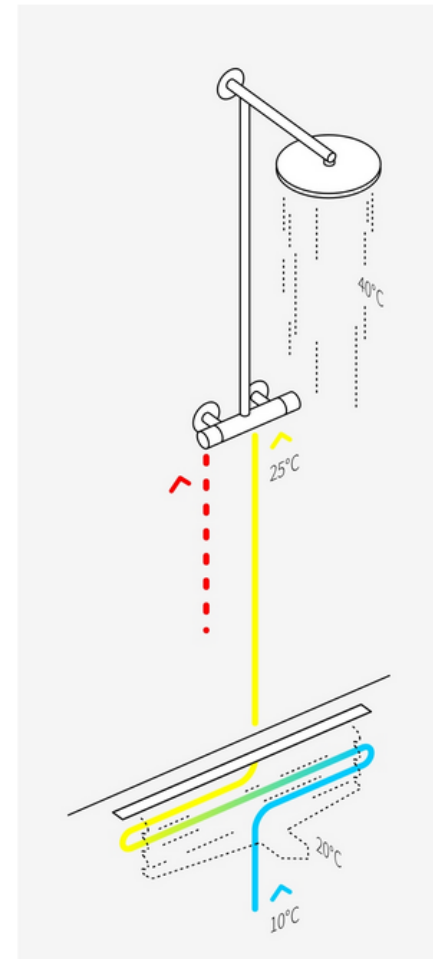
Thanks to the rerouting of the cold water...

The Joulia-Inline shower drain is directly connected to the cold water pipes. Thanks to the integrated heat recovery, the heat of the used water...

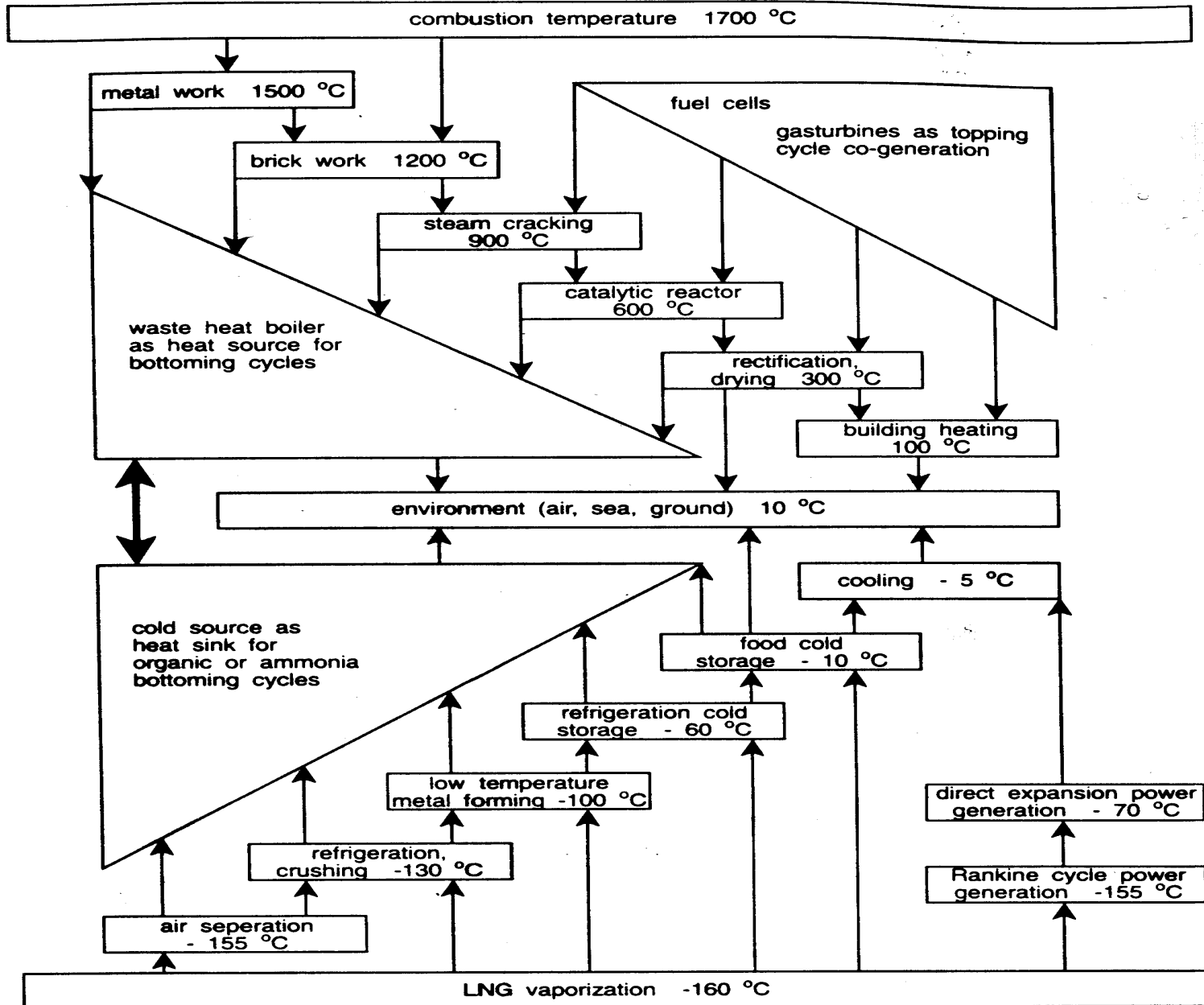


... the heat energy comes back!

...preheats the fresh cold water. Thereby less warm water is needed in the mixing valve and a lot of CO₂ and money can be saved.



Minimizing energy losses by “cascading”



Heat Integration

Pinch Technology

Course Introduction: Heat integration

Objective	To introduce the problem of process heat recovery and Pinch analysis for solving this problem.
Scope	The course will focus on energy targets, the Pinch Design method, capital cost targeting and the integration of heat pumps.
Assumed Background	Basic thermodynamics
Recommended reading	Smith, <i>Chemical Process Design</i> , 1995, McGraw-Hill

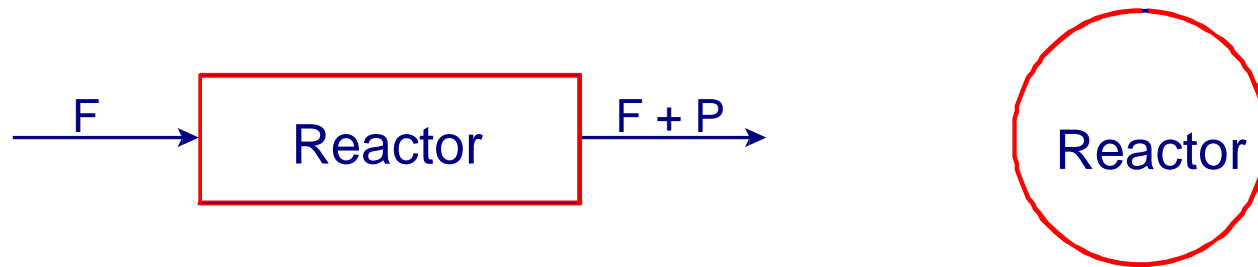
Contents

- Part 1 Introduction
- Part 2 Setting Energy Targets
and the Graphical Approach
- Part 3 The Problem Table Algorithm
and Grand Composite Curve
- Part 4 Integration of Heat Pumps

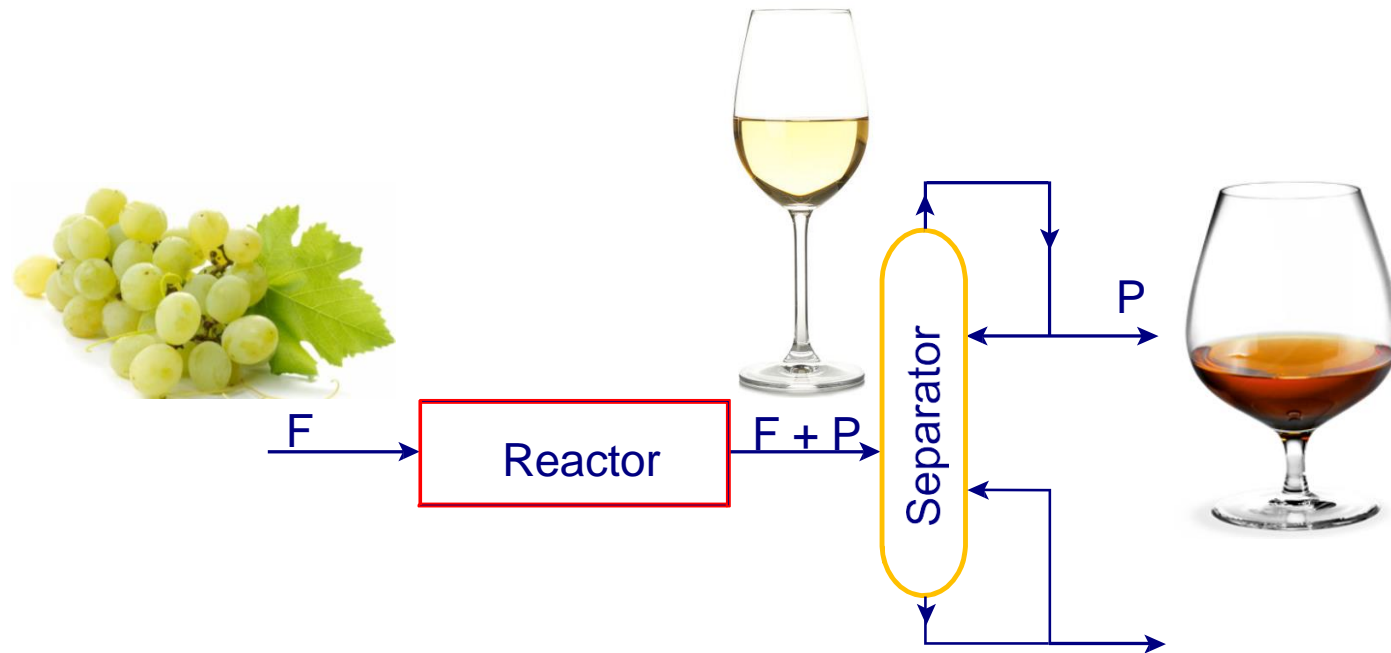
Part 1

Introduction - Heat Integration

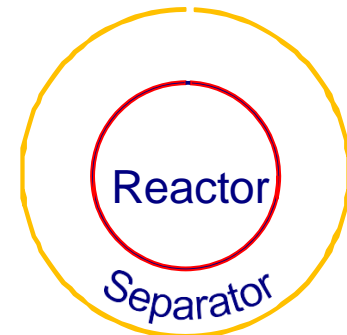
Let's start by considering the
hierarchy of process design

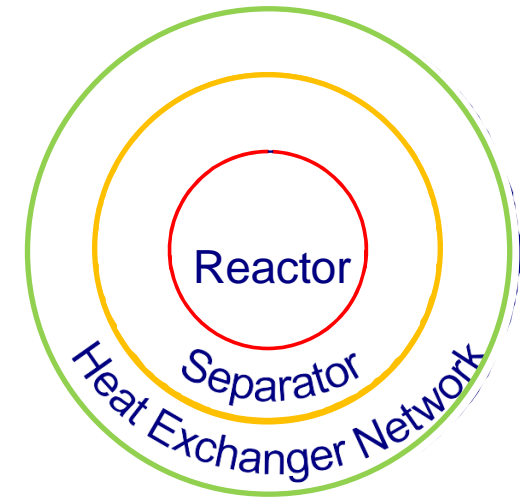
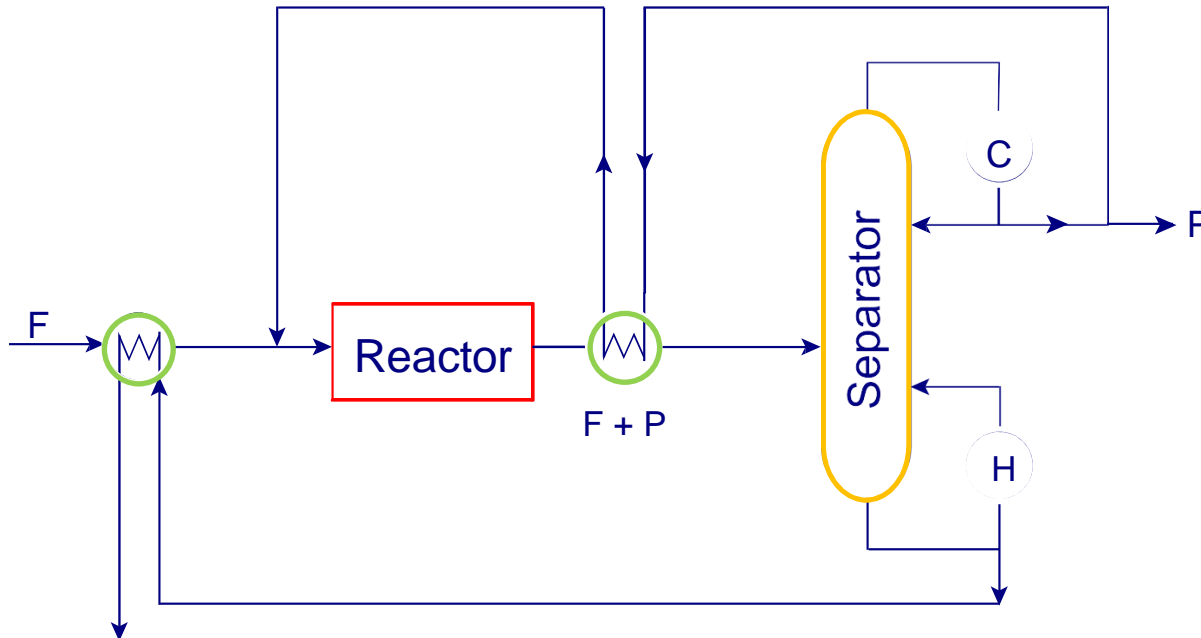


Process design starts with the reactor

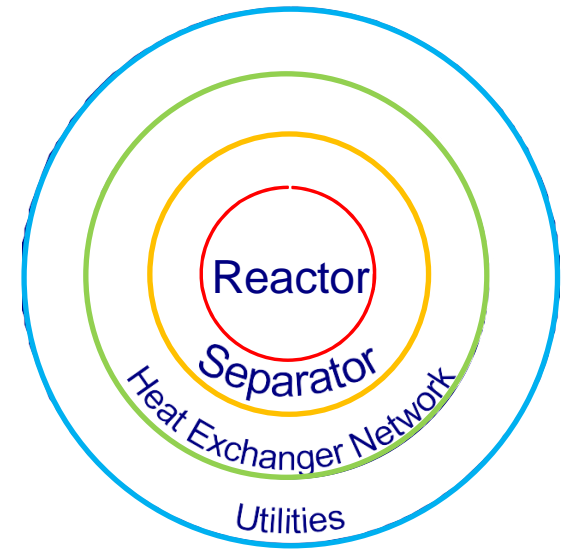
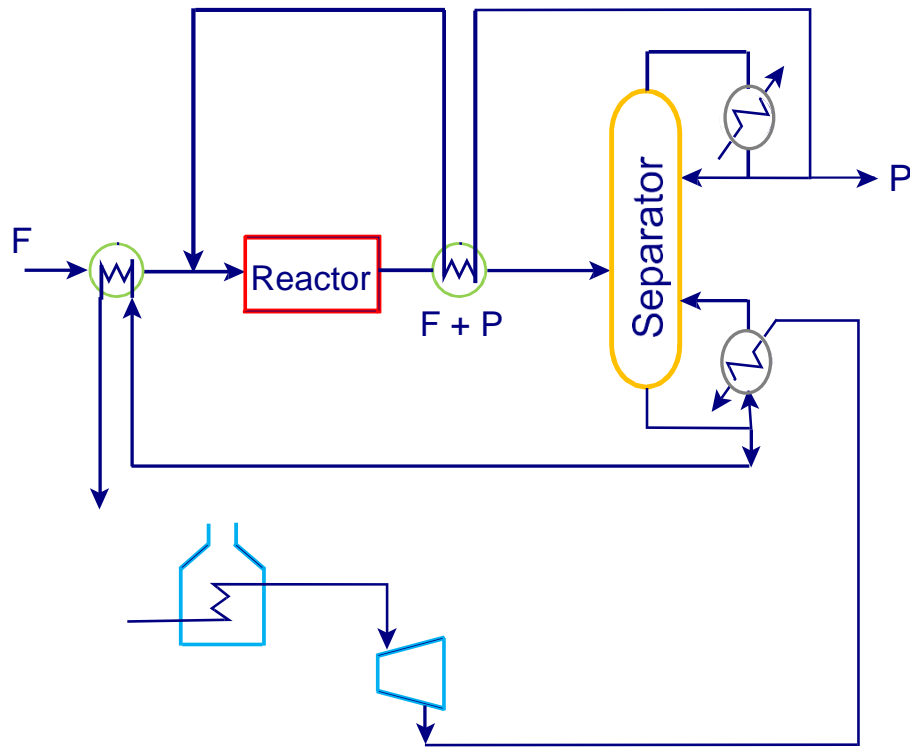


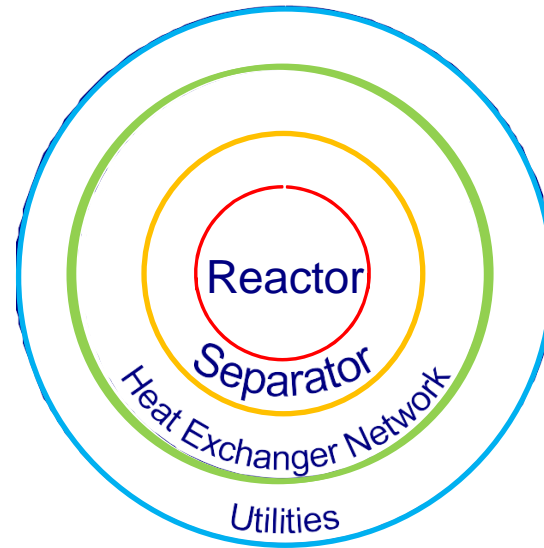
Once we know the reactor design,
we need to specify the separation system





Once we know reactor and separator design, we know
material and energy balance - Heat Exchanger Network





The "Onion" Diagram

What is better process integration about?

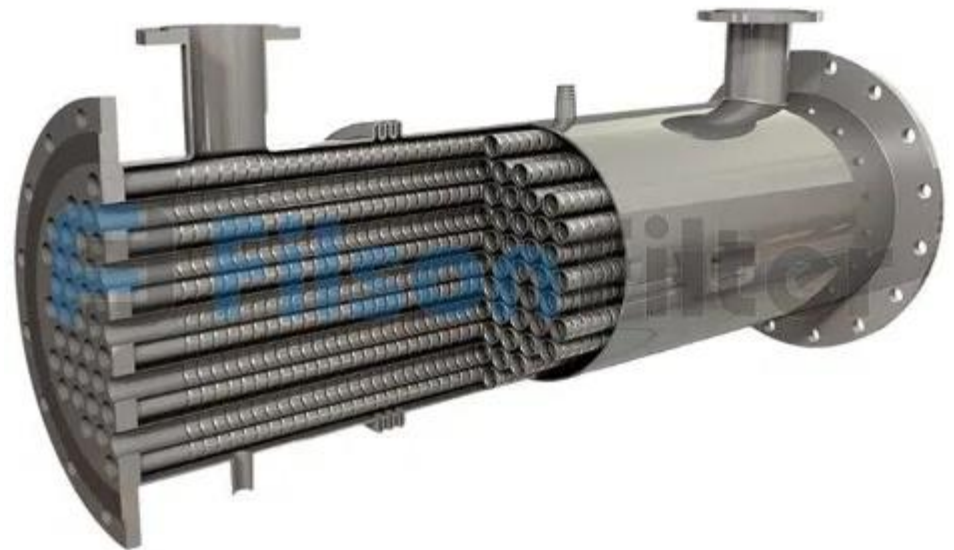
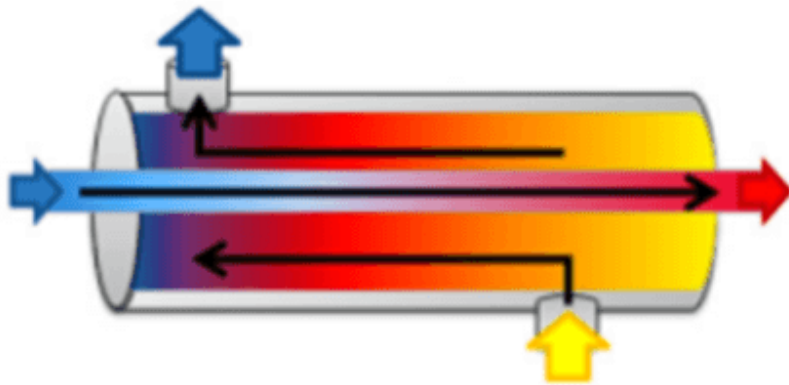
- Better process design
- Increased throughput in retrofit
- Reduced utility costs
- Better utilisation of capital
- Reduced emissions

The Basic Terminology

Heat recovery: Heat exchanger

Echangeur de chaleur

Counter-Current Flow

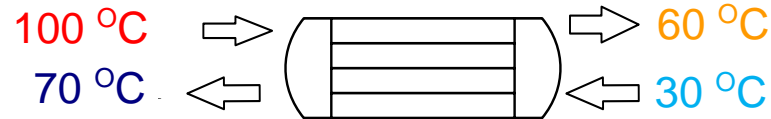


<https://www.google.com/search?q=counter-current+heat+exchanger&tbm=isch>
<https://www.filsonfilters.com/counter-flow-heat-exchanger/>

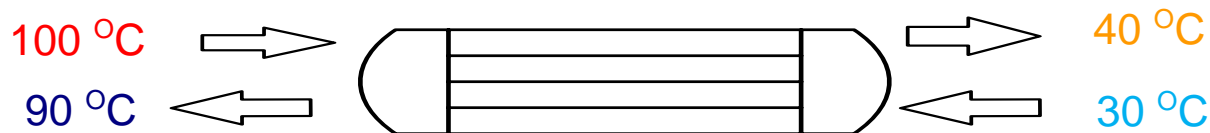
Heat recovery:

Small versus large heat exchanger (here: counterflow)

Echangeur de chaleur – petit ou grand (ici: contre-courant)



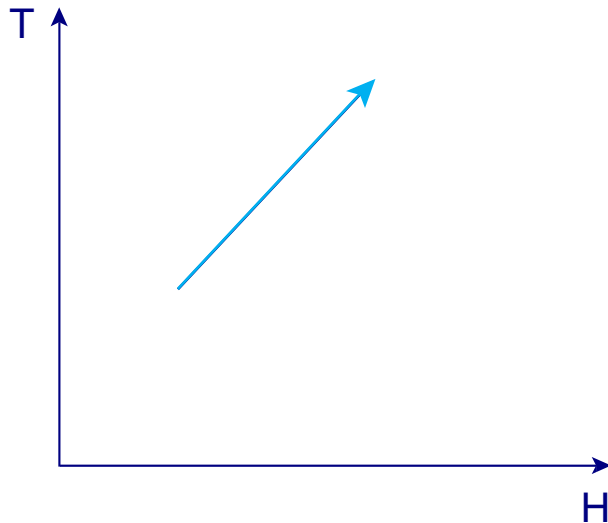
$$\Delta H = m \cdot c_p \cdot \Delta T$$



→ Which heat exchanger would you prefer (for using waste heat at 100 °C)?

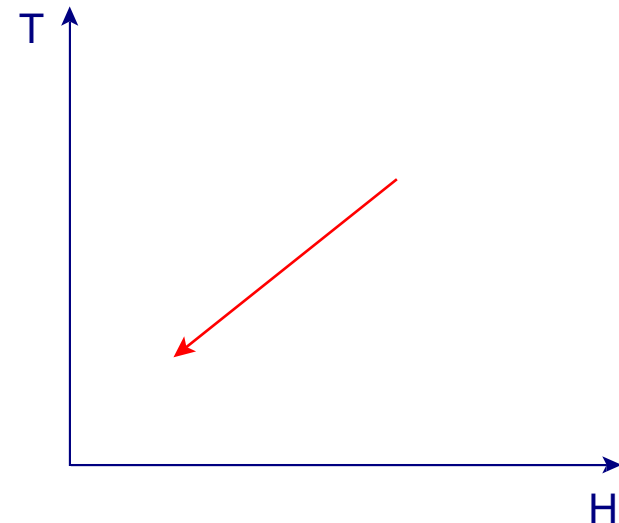
The Streams

" Cold " streams require heating
(Courants froids)



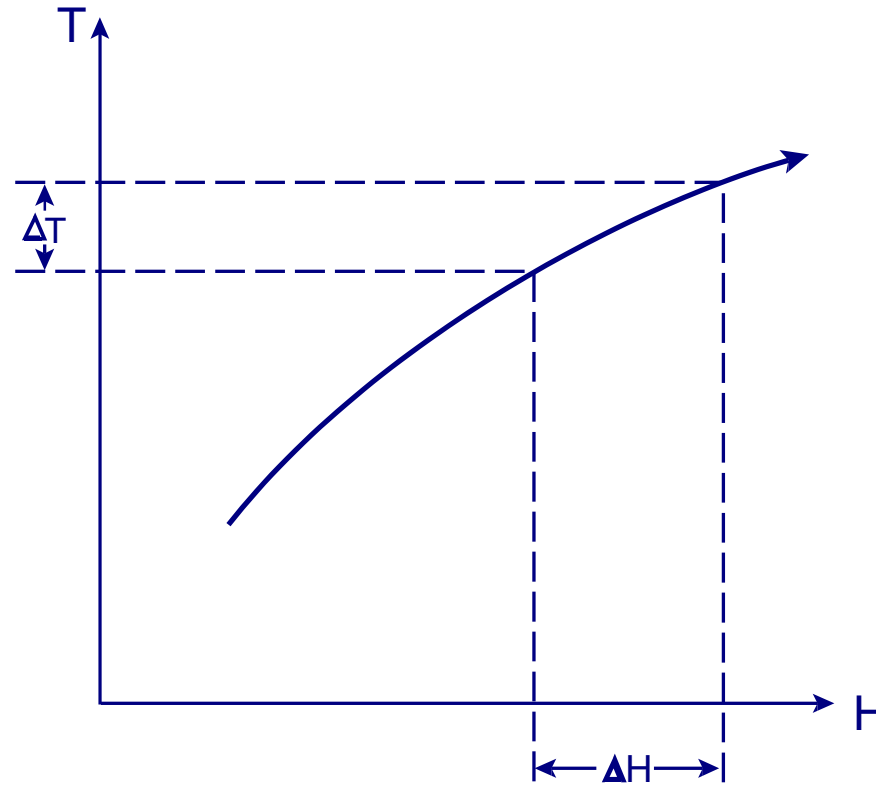
Example: Fresh milk needs to be heated up as part of the ultra-high temperature (UHT) treatment.

" Hot " streams require cooling
(Courants chauds)



Example: Milk that has undergone ultra-high temperature treatment needs to be cooled down before packaging.

Temperature-Enthalpy Diagram



H = Stream Enthalpy (MW or kW)

Heat Duties (Charge thermique)

$$\Delta H = m \cdot c_p \cdot \Delta T$$

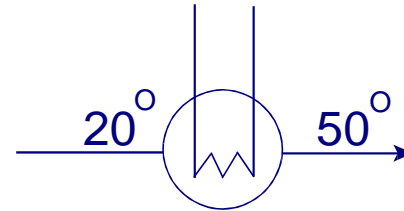
$$m \text{ [kg/s]}$$

$$c_p \text{ [MJ/(}^\circ\text{C}\cdot\text{kg)]}$$

$$\Delta T \text{ [}^\circ\text{C]}$$

$$\Delta H \text{ [MW]}$$

$$CP = m \cdot c_p = \frac{\Delta H}{\Delta T}$$



$$CP = 0.5 \text{ [MW/}^\circ\text{C]}$$

$$\Delta H = 0.5 \cdot 30 \text{ [MW]}$$

$$\Delta H = CP \cdot \Delta T$$

Heat Capacity
Flowrate

(débit de capacité
de chaleur)



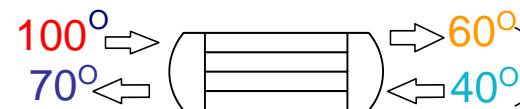
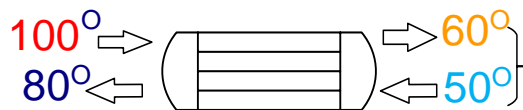
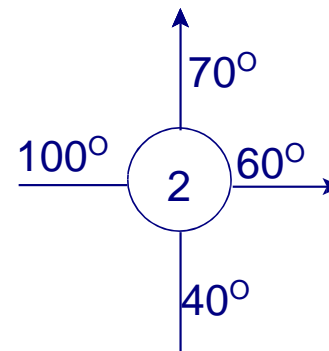
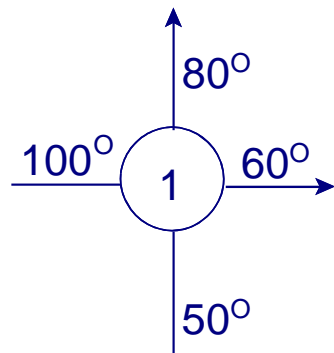
CP = Product of mass flow (m)
and specific heat capacity (c_p)
→ [MW/°C]

(débit massique)
(chaleur spécifique)

$$\Delta T_{\min}$$

(Différence de température minimale)

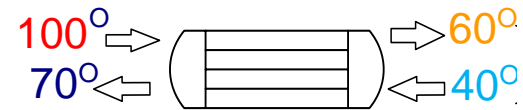
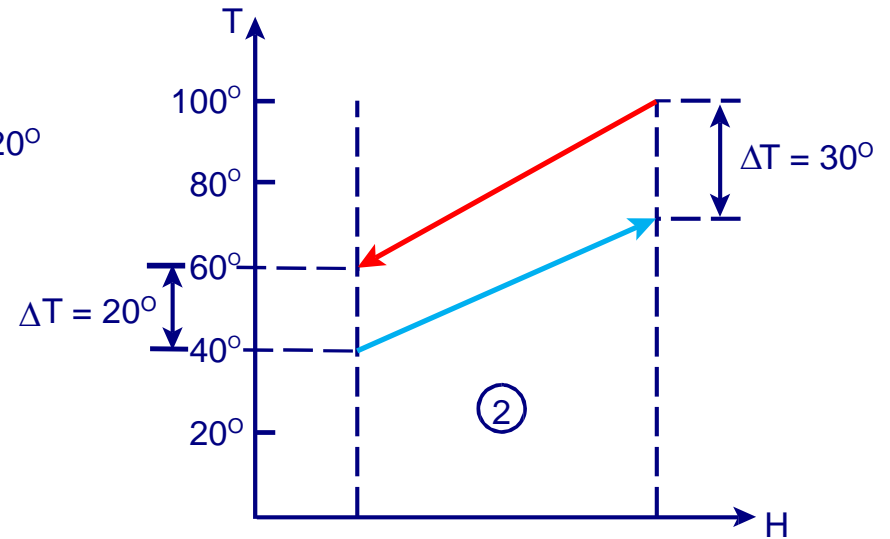
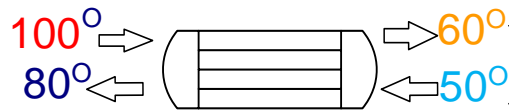
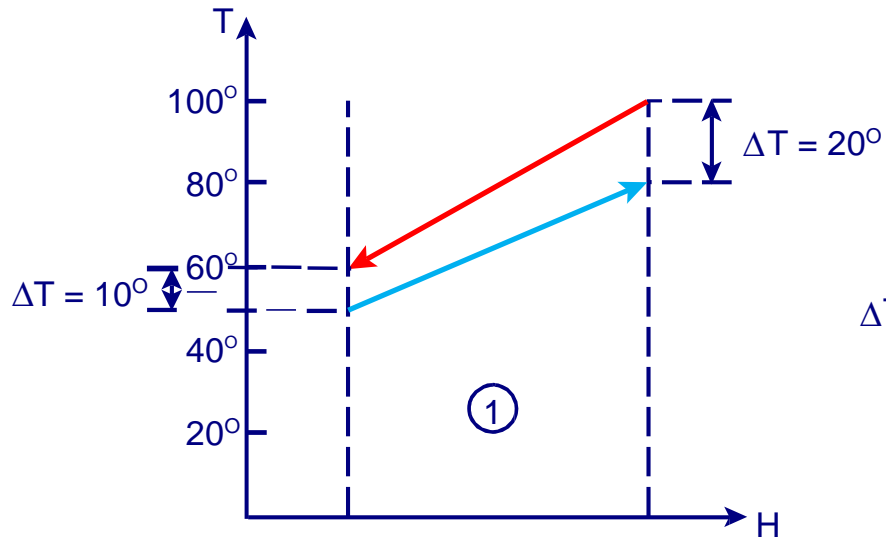
Minimum Permissible Temperature Difference



$$\Delta T_{\min} = 20^\circ$$

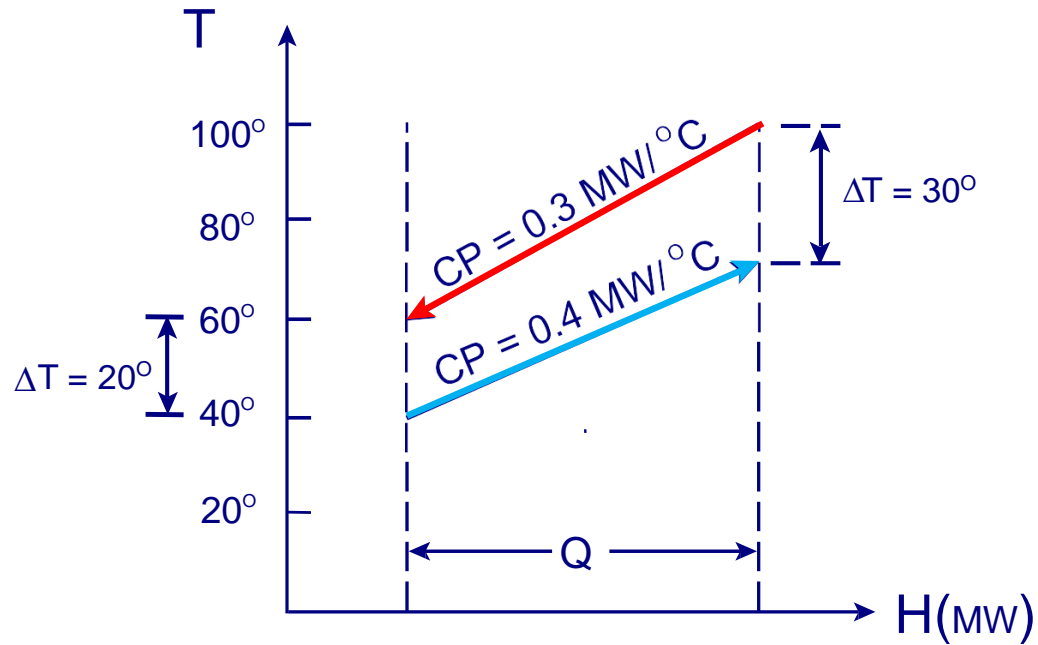
Which heat exchanger violates ΔT_{\min} ?

(Échangeur de chaleur)



$$\Delta H = CP \cdot \Delta T$$

Heat Exchanger Duty



$$\begin{aligned}
 Q &= |\Delta H| = CP \times \Delta T \\
 &= 0.3 \times 40 \\
 &= 0.4 \times 30 \\
 Q &= 12 \text{ MW}
 \end{aligned}$$

Part 2

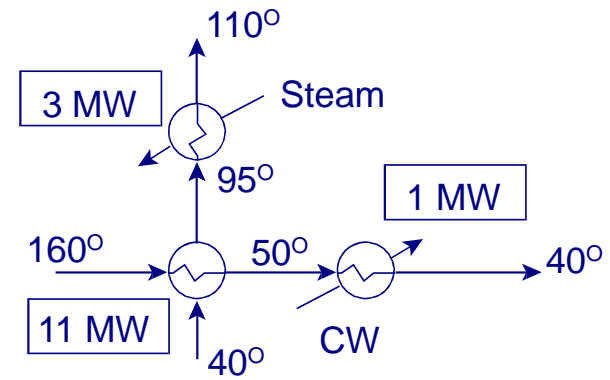
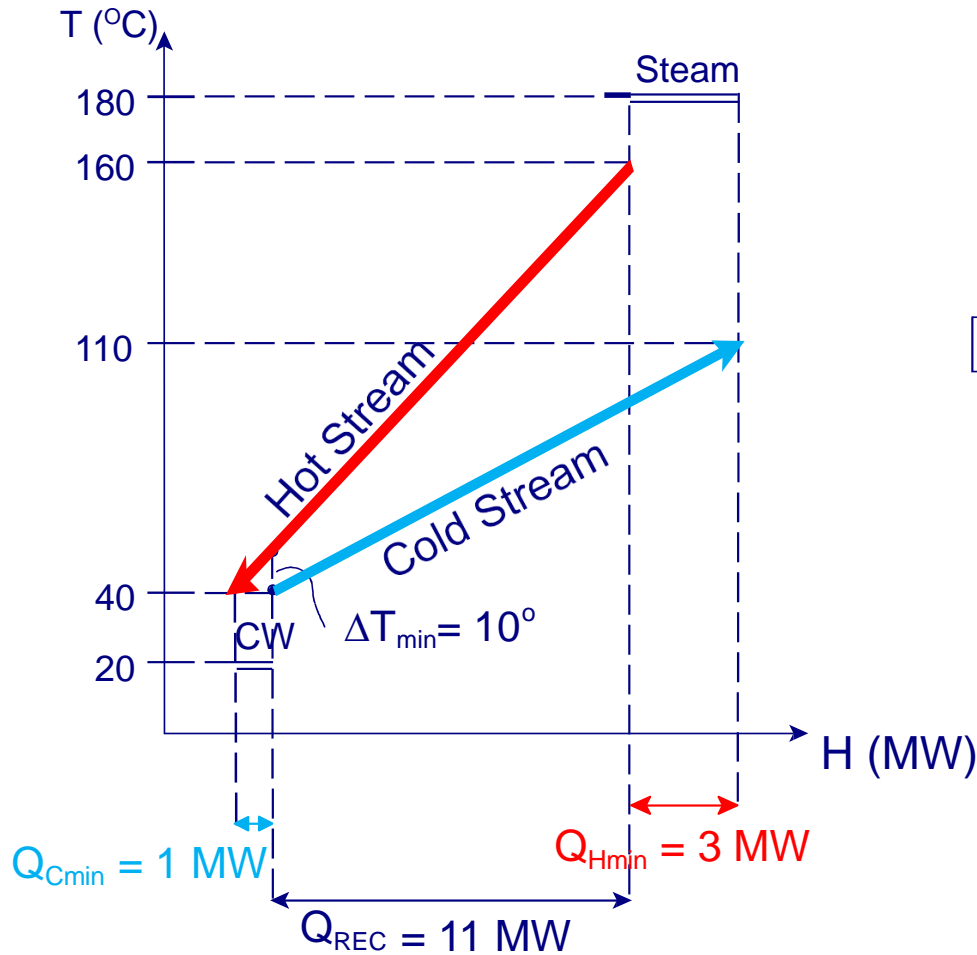
Setting Energy Targets

Two-Stream Heat Recovery Problem

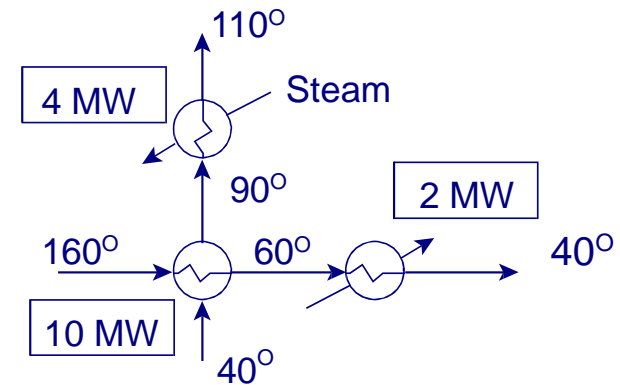
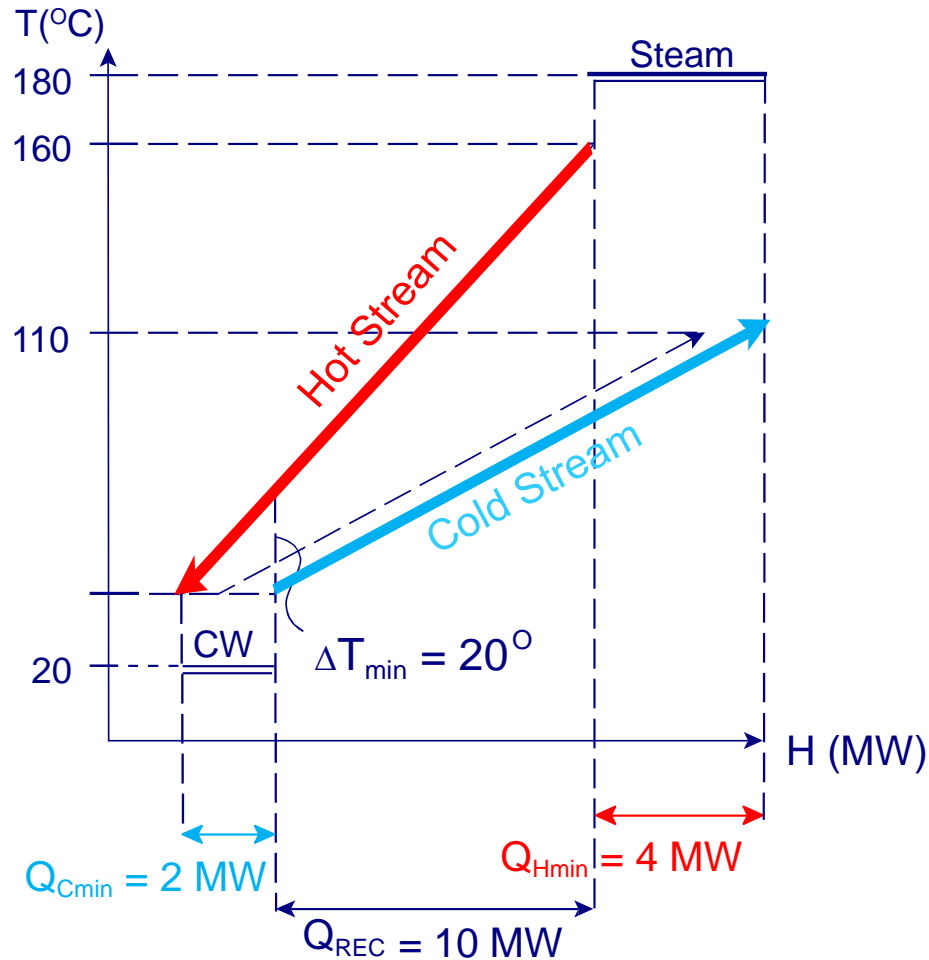
Stream	Type	Supply Temp. T (°C)	Target Temp. T (°C)	CP (MW/°C)	ΔH (MW)
1	Cold	40	110	0.2	14
2	Hot	160	40	0.1	-12

$$\Delta H = CP \cdot \Delta T$$

Two-Steam Heat Recovery Problem



Streams can be shifted horizontally



Two Basic Facts

- Correlation between

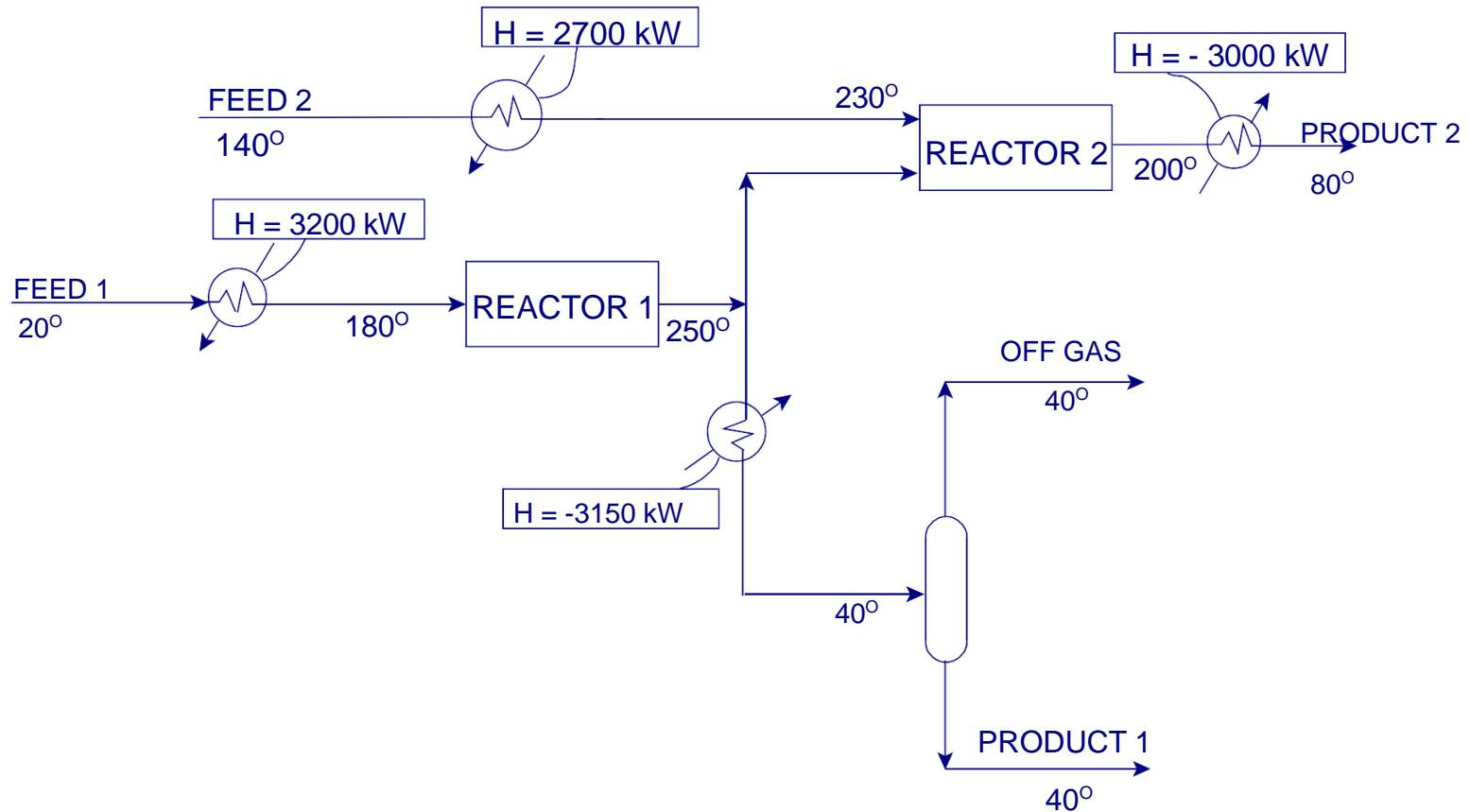
ΔT_{\min} and Q_{Hmin} , Q_{Cmin}

- More in, More Out !

$$Q_{\text{Hmin}} + X \longrightarrow Q_{\text{Cmin}} + X$$

What if several hot and
several cold streams?

Example 2

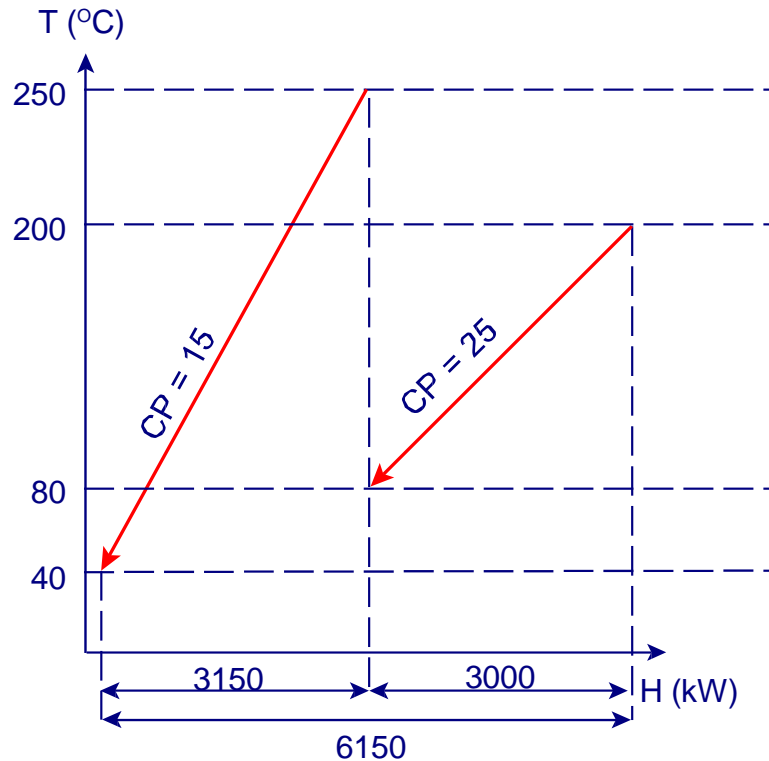


A simple flowsheet with two hot streams and two cold streams.

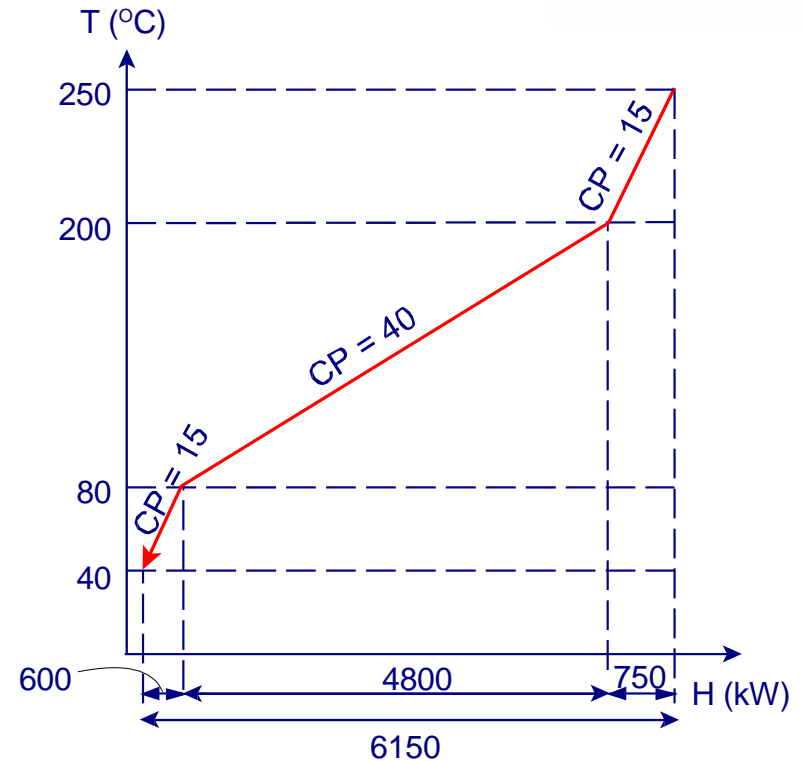
Stream Data from the Flowsheet

Stream	Type	Supply Temp. T_S (°C)	Target Temp. T_T (°C)	ΔH (kW)	Heat Capacity Flowrate CP (kW °C ⁻¹)
Reactor 1 feed	Cold	20	180	3200	20
Reactor 1 product	Hot	250	40	-3150	15
Reactor 2 feed	Cold	140	230	2700	30
Reactor 2 product	Hot	200	80	-3000	25

$$\Delta H = CP \cdot \Delta T$$

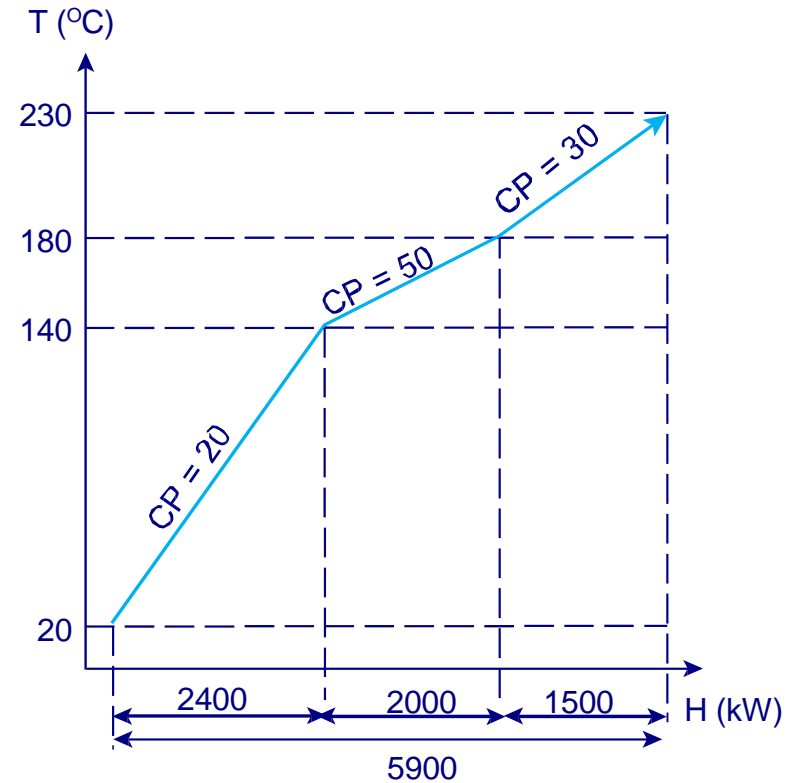
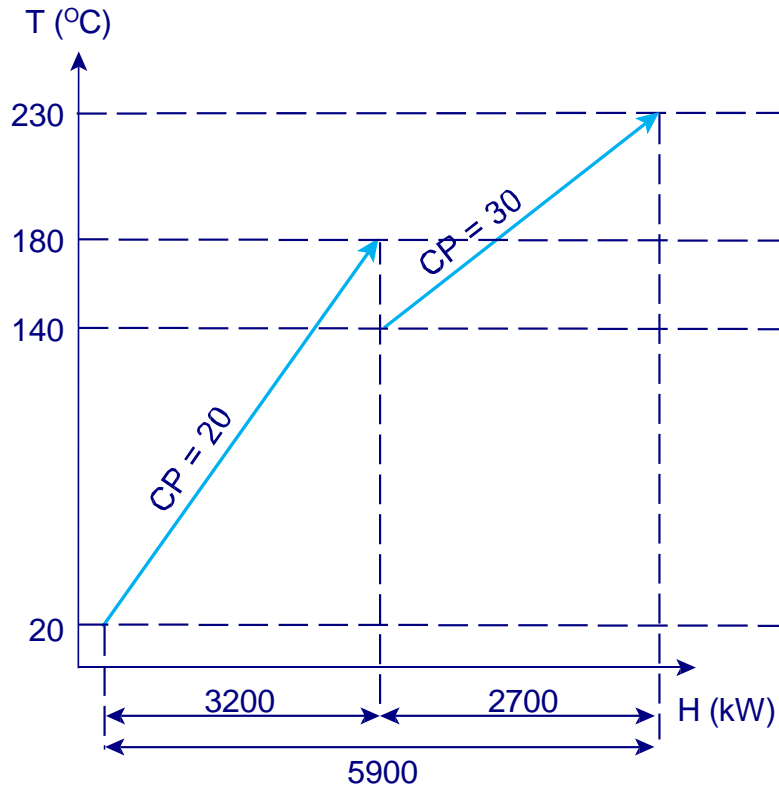


(a) The hot streams plotted separately



(b) Hot composite curve

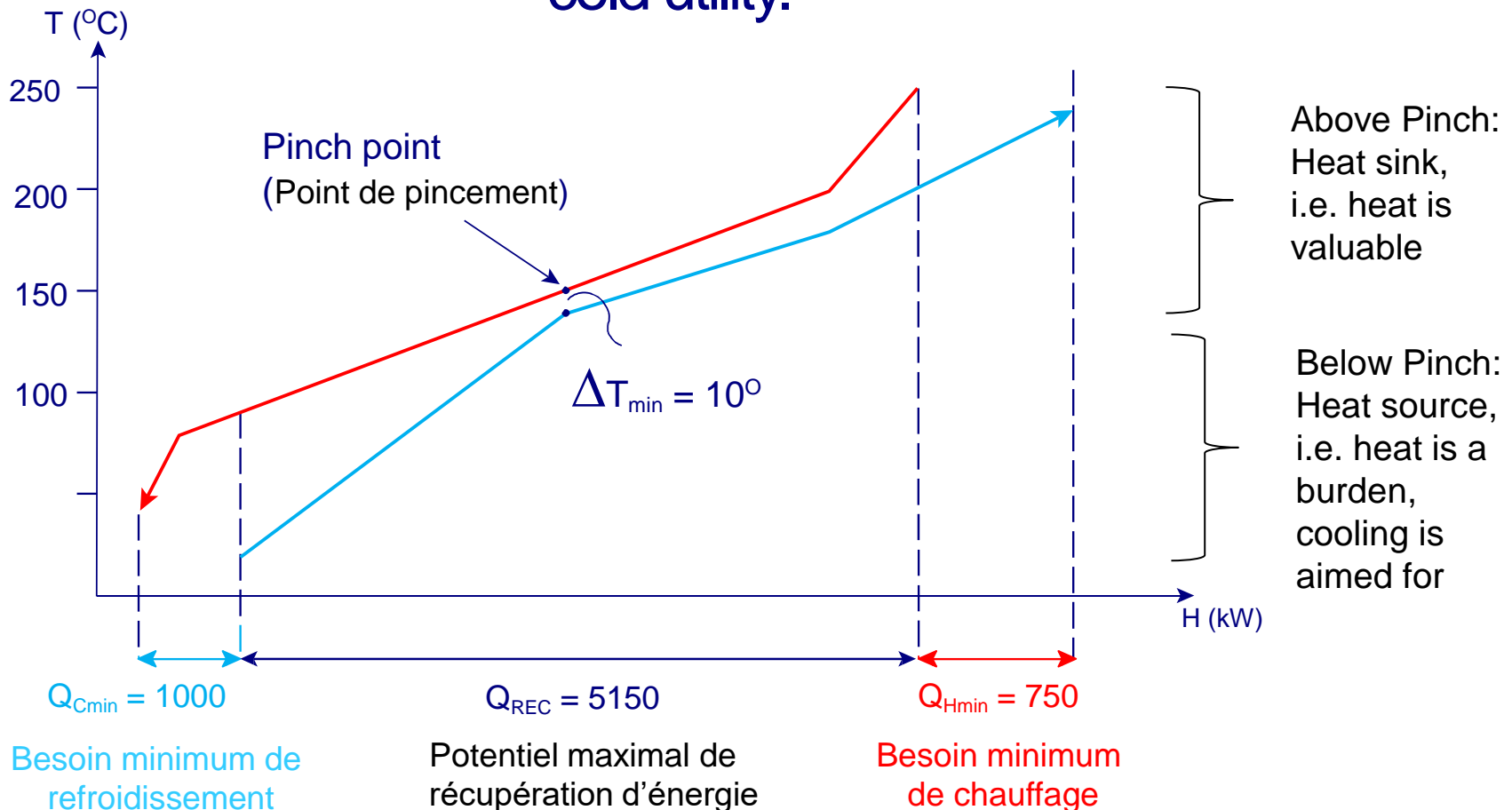
Add the heat available in each temperature interval to form a composite curve.



(a) The cold streams plotted separately (b) Cold composite curve

The cold streams can also be combined to obtain a composite cold stream.

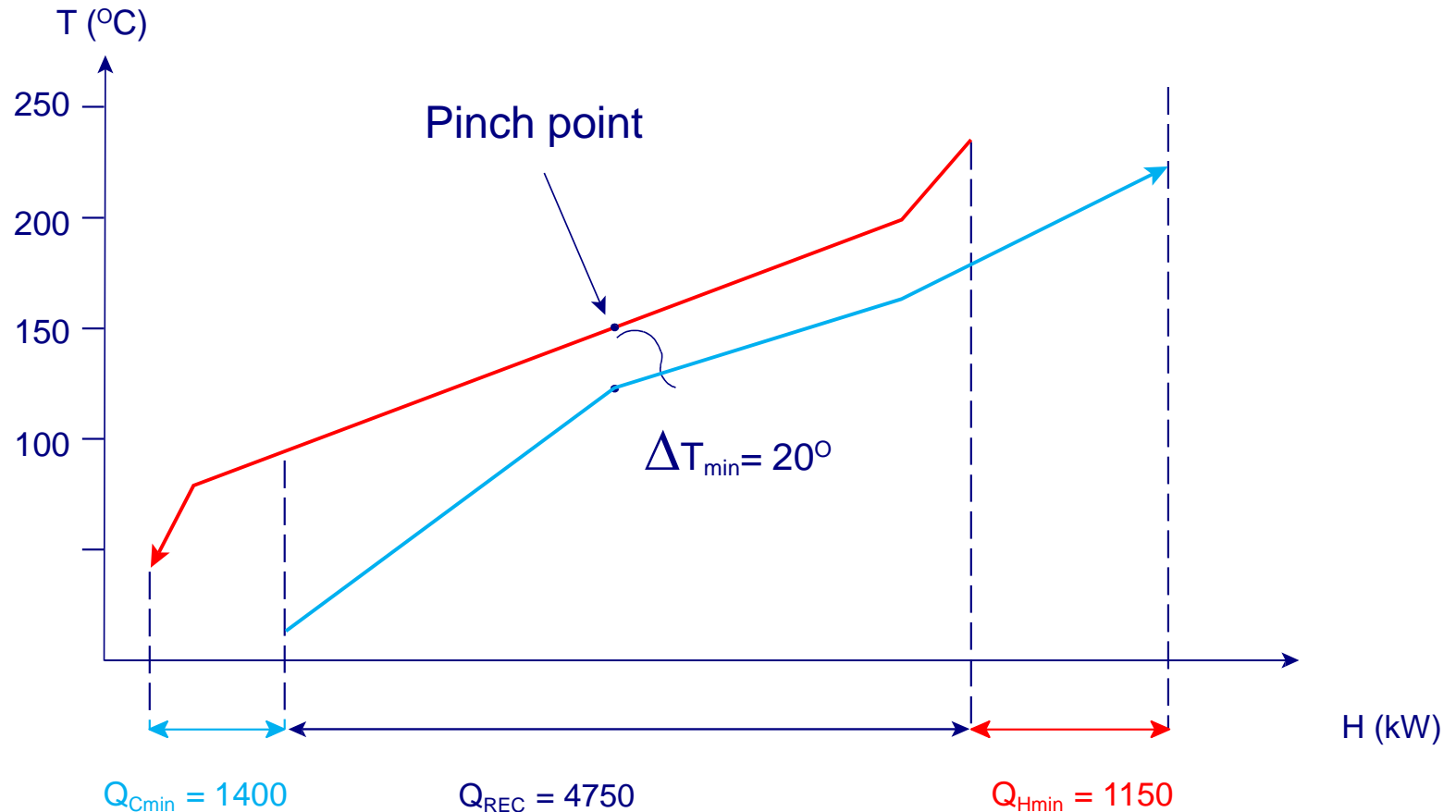
Plotting the hot and cold composite curves together gives the targets for hot and cold utility.



Golden rules:

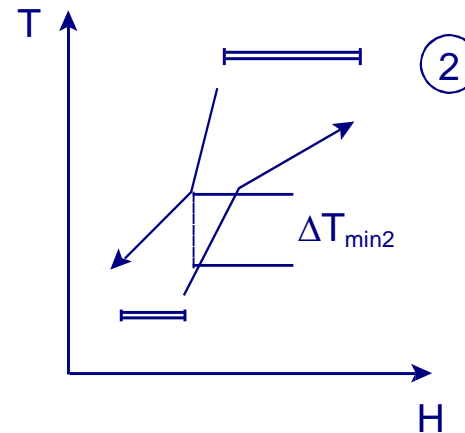
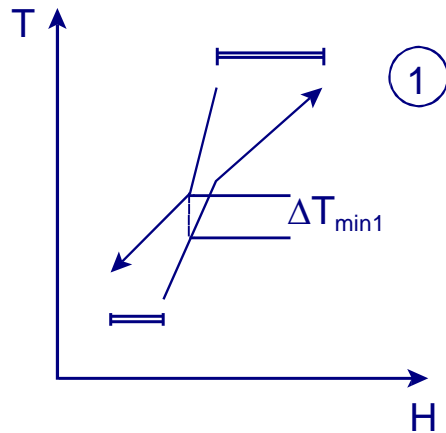
- Don't transfer heat across the pinch
(from hot to cold area)
- Don't use cold utilities above the pinch
- Don't use hot utilities below the pinch

Now increase ΔT_{\min} to 20°C

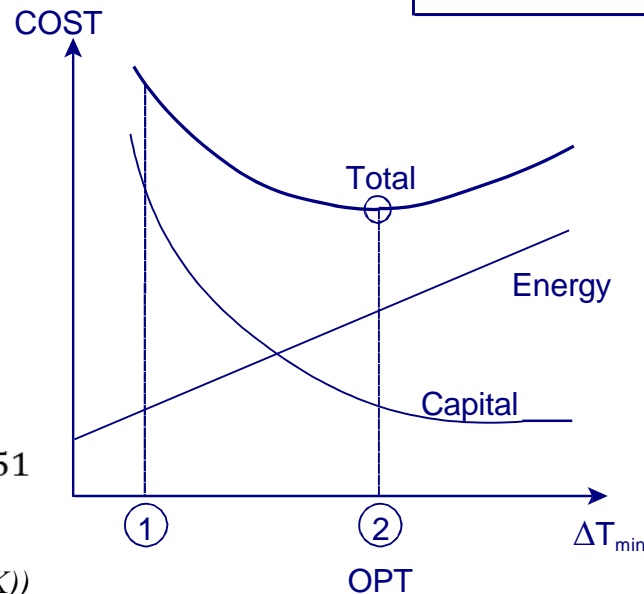


$Q_{H\min}$ and $Q_{C\min}$ increase correspondingly

Choice of ΔT_{min} is nowadays subject to economic trade-off



On the one hand:
smaller ΔT_{min}
→ less heating and cooling (①, ②)



On the one hand:
smaller ΔT_{min}
→ smaller heat flow
in heat exchanger
→ H. exch. must be
larger
→ H. exch. becomes
more expensive

$$Q_{saved} = U \cdot A \cdot \Delta T_{min}$$

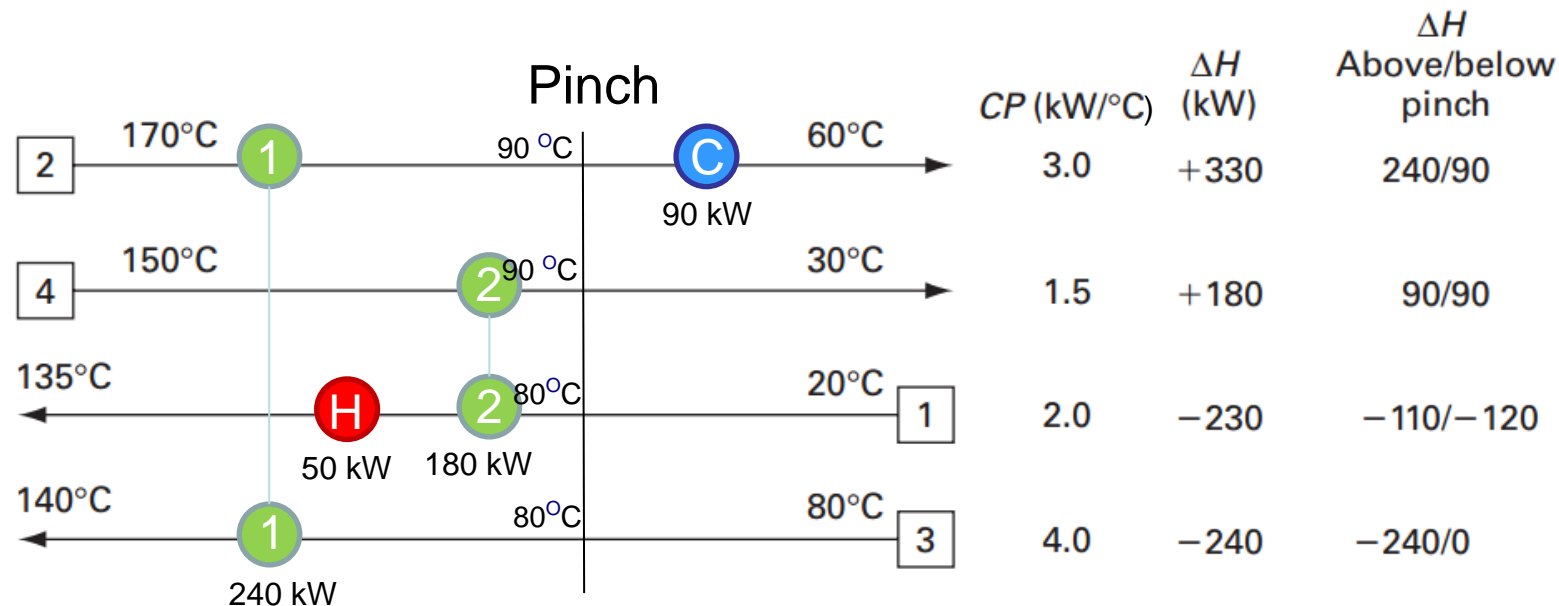
$$Cost_{exch} = 1957.8 * [A]^{0.551}$$

U = Overall heat transfer coefficient ($W/(m^2 \cdot K)$)

A = Surface area (m^2)

ΔT_{min} = minimum (pre-set) temperature difference

How do you design the network with your common sense?

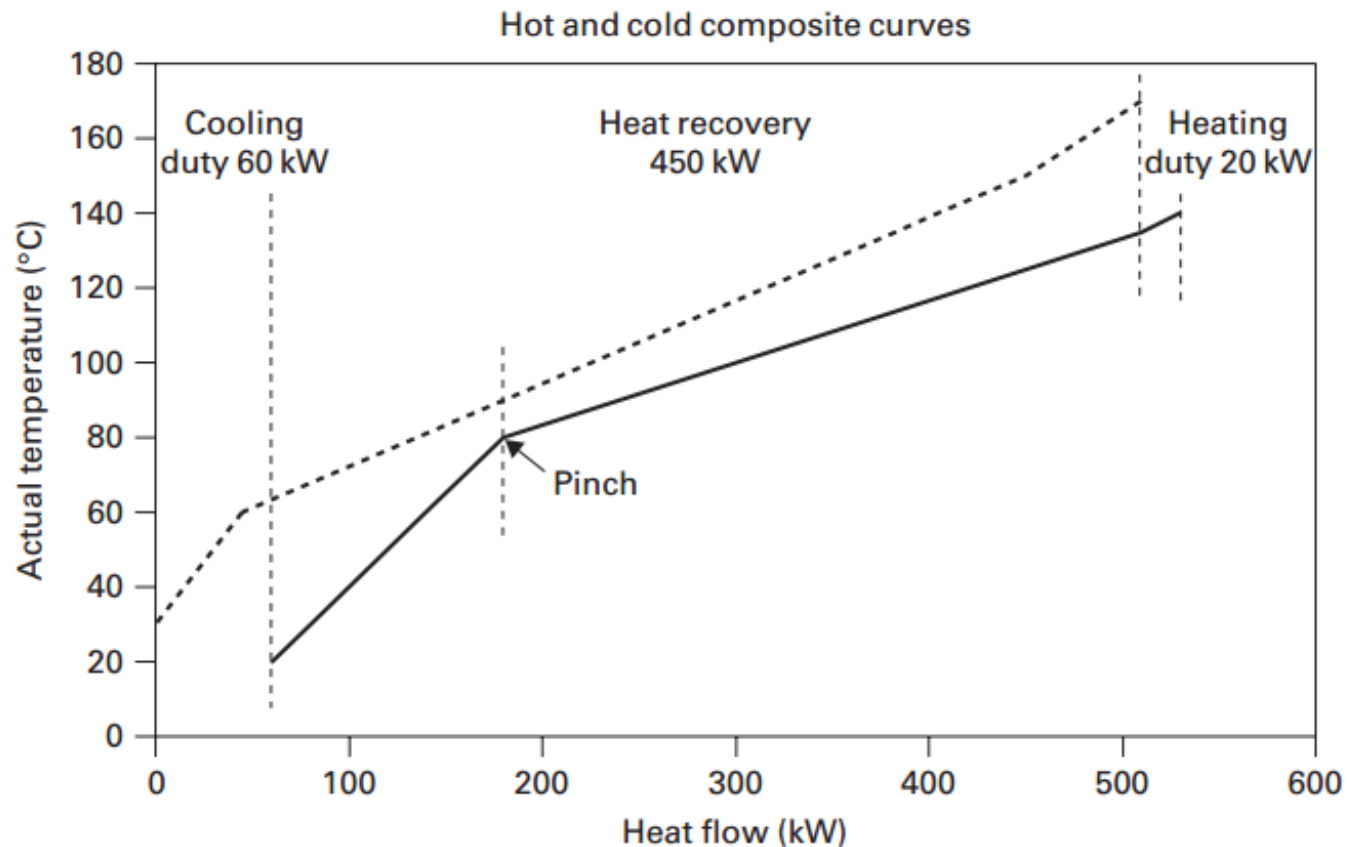


Above: $240 + 90 - 110 - 240 = -20$
 Below: $90 + 90 - 120 - 0 = 60$

30 kW is being transferred across the pinch!

“Traditional” heat exchanger network designs are almost invariably off-target

How much energy would the ideal network have needed? (1/2)



How much energy would the ideal network have needed? (2/2)

Problem table algorithm									
Interval i	Temperature Intervals	Stream population	$\Delta T_{\text{interval}} (\text{°C})$	$\Sigma \text{CP cold} - \Sigma \text{CP hot} (\text{kW/°C})$	$\Delta H_{\text{interval}} (\text{kW})$	Surplus or deficit	Cascade heat flow (kW), uncorrected	Cascade heat flow (kW), corrected	
	165						0	20	Min. heating duty
1	145	2	20	-3	-60	surplus	60	80	
2	140	4	5	-0.5	-2.5	surplus	62.5	82.5	
3	85	3	55	1.5	82.5	deficit	-20	0	Pinch
4	55	1	30	-2.5	-75	surplus	55	75	
5	25		30	0.5	15	deficit	40	60	Min. cooling duty

Summary

- Temperature-enthalpy diagrams can be used to determine heat recovery potential
- Composite curves can be used to simultaneously analyze a set of hot streams and cold streams
- Energy targets are determined based on energy balance and ΔT_{\min} .
- Energy targets can be varied by changing ΔT_{\min} .

Part 3

The Problem Table Algorithm
and Grand Composite Curve

Stream Data, ΔT_{\min}



"Composite Curves"



Energy Targets

But Composite Curves are
complicated

An Alternative:

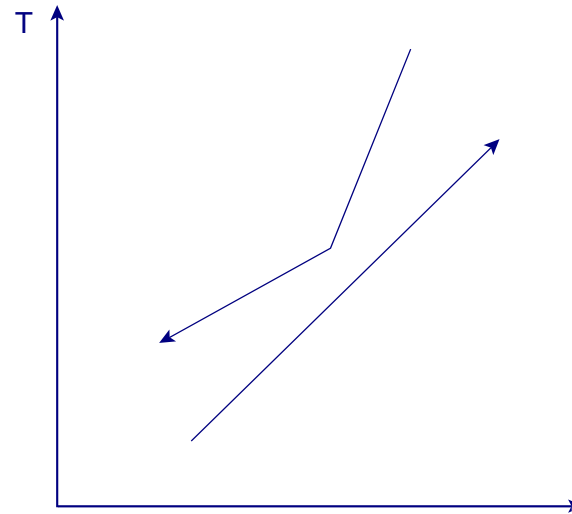
"The Problem Table"

Example 2

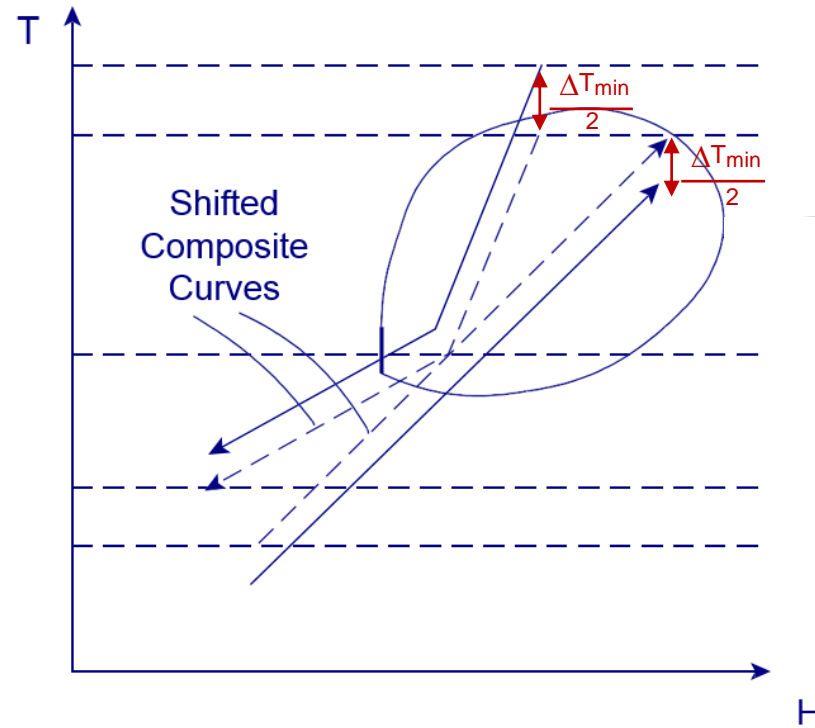
Stream Data Table

No	Stream	Type	Supply Temp. T_S ($^{\circ}\text{C}$)	Target Temp. T_T ($^{\circ}\text{C}$)	Enthalpy change ΔH (kW)	Heat Capacity Flowrate CP ($\text{kW } ^{\circ}\text{C}^{-1}$)
1	Reactor 1 feed	Cold	20	180	3200	20
2	Reactor 1 product	Hot	250	40	-3150	15
3	Reactor 2 feed	Cold	140	230	2700	30
4	Reactor 2 product	Hot	200	80	-3000	25

Shift Composite Curves



Shift Composite Curves



Shifting rule:

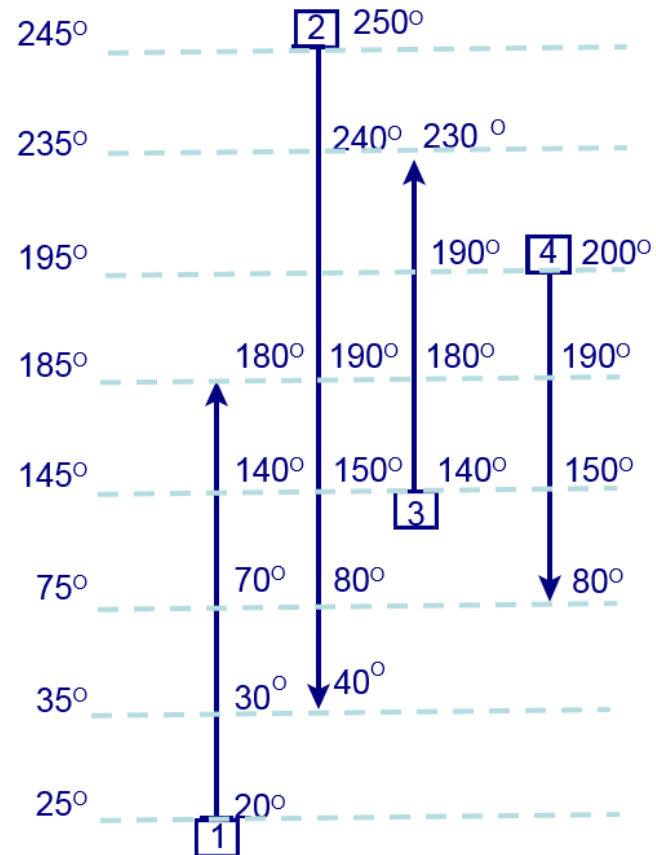
$$\begin{array}{l} \text{Cold streams} \quad + \quad \frac{\Delta T_{\min}}{2} \\ \text{Hot streams} \quad - \quad \frac{\Delta T_{\min}}{2} \end{array}$$

Stream data for
our example:

Stream No	Type	T_S (°C)	T_T (°C)	T_S^* (°C)	T_T^* (°C)
1	Cold	20	180	25	185
2	Hot	250	40	245	35
3	Cold	140	230	145	235
4	Hot	200	80	195	75

Shifted temperature intervals

T^* Interval
Temperature
($^{\circ}\text{C}$)



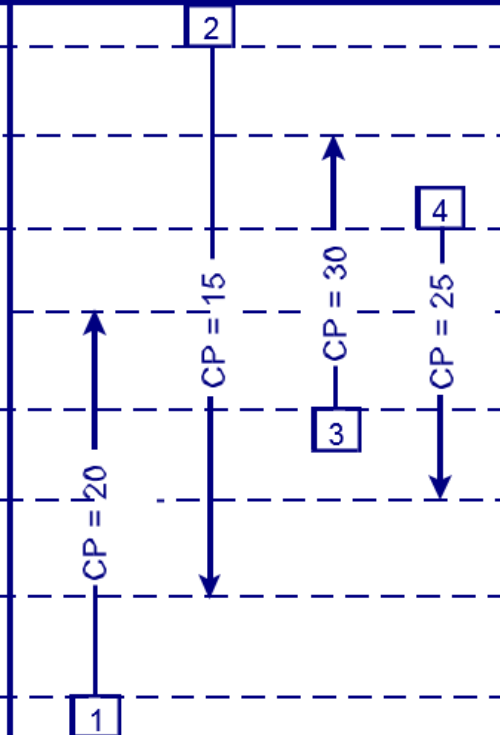
In each shifted temperature interval,
calculate a simple energy balance from

$$\Delta H_i = \left(\sum_{\text{All cold streams}} CP_C - \sum_{\text{All hot streams}} CP_H \right)_i \Delta T_i$$

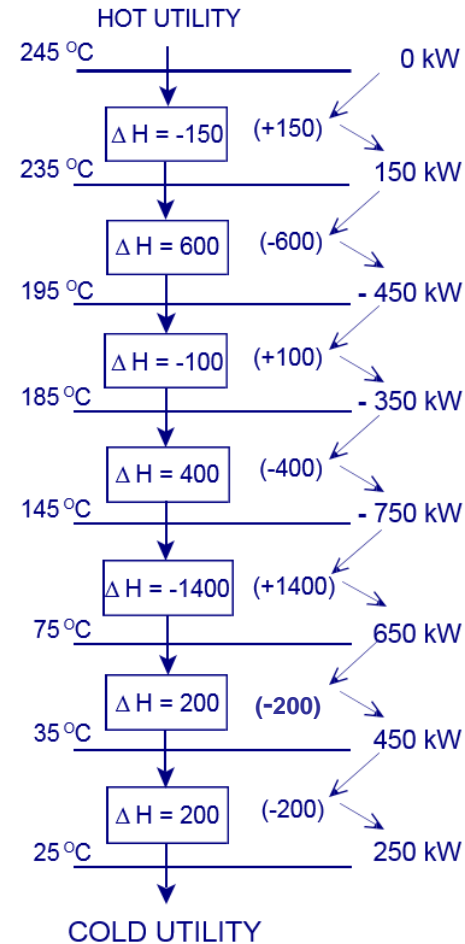
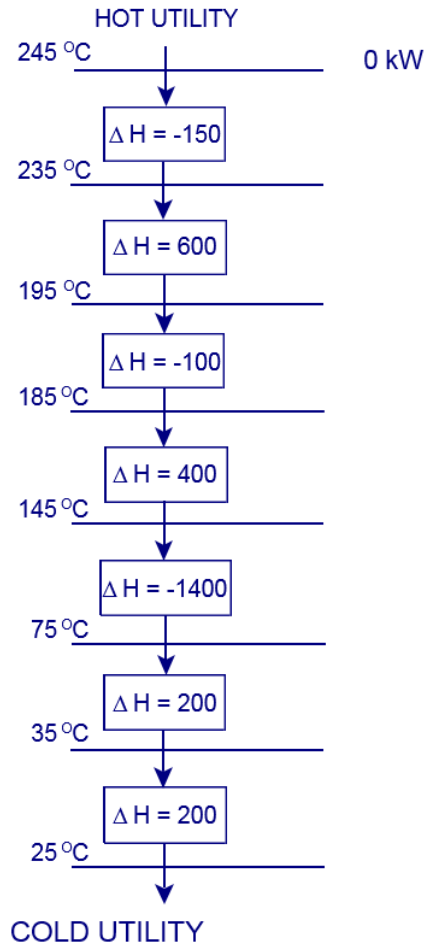
- ΔH_i = heat balance for interval
- ΔT_i = temperature difference across interval

Problem table (for Temperature Interval Heat Balance)

Interval Temperature	Stream Population	$\Delta T_{\text{INTERVAL}}$ (°C)	$\sum CP_C$ $-\sum CP_H$ (kW/°C)	$\Delta H_{\text{INTERVAL}}$ (kW)	Surplus/ Deficit
245°	2				
235°		10	-15	-150	Surplus
195°		40	15	600	Deficit
185°		10	-10	-100	Surplus
145°		40	10	400	Deficit
75°		70	-20	-1400	Surplus
35°		40	5	200	Deficit
25°	1	10	20	200	Deficit

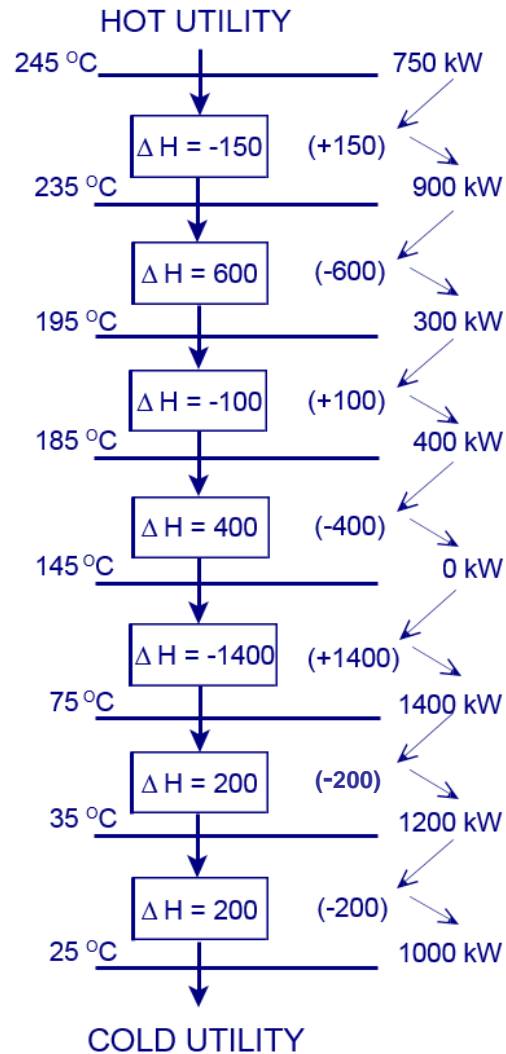


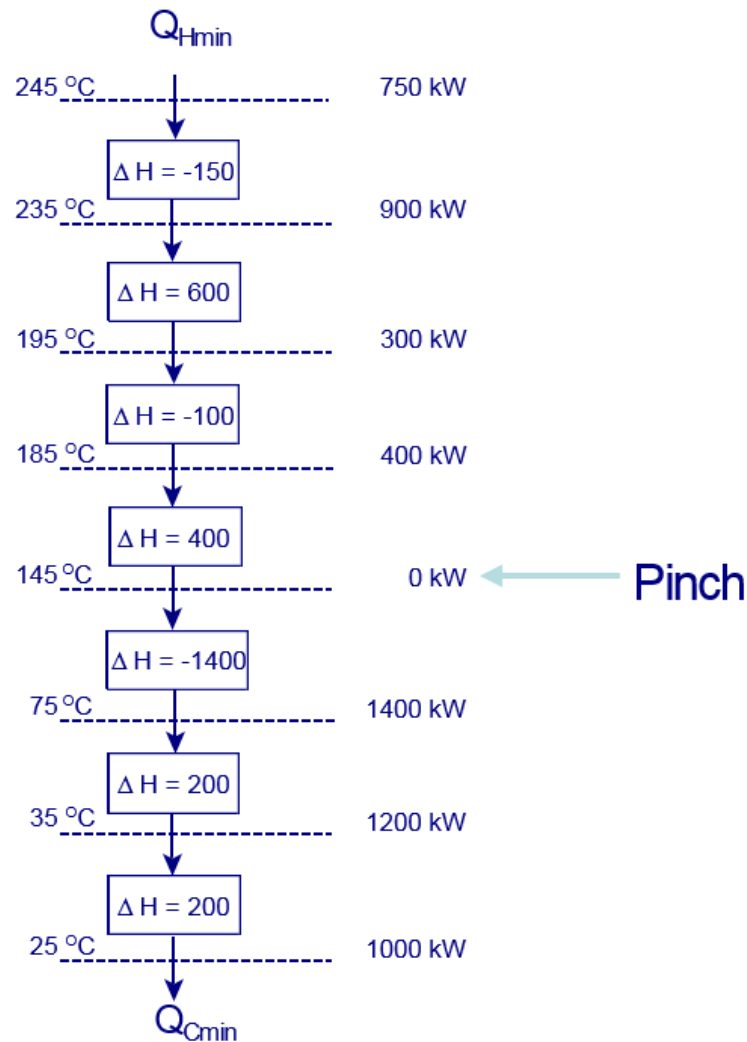
Cascade any surplus heat from high to low temperature



Problem table cascade

Heat flows cannot be negative! Add heat to make them at least 0!





$T^*_{\text{pinch}} = 145^\circ\text{C}$
 $T_{\text{pinch}} = 150^\circ\text{C}$ for hot streams
 $T_{\text{pinch}} = 140^\circ\text{C}$ for cold streams

Summary

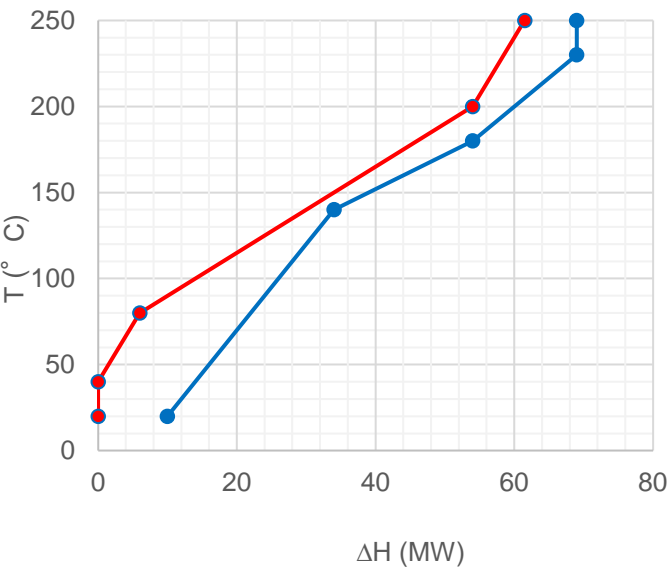
- The problem table algorithm:
 - STEP 1
 - Adjust For ΔT_{\min}
 - STEP 2
 - Set Up Temperature Intervals
 - STEP 3
 - Calculate Interval Heat Balances
 - STEP 4
 - Cascade For Positive Heat Flows
- $Q_{H\min}$, $Q_{C\min}$ and pinch location without drawing graphs

How do we target for the best
mix of utilities?

- The Grand Composite Curve

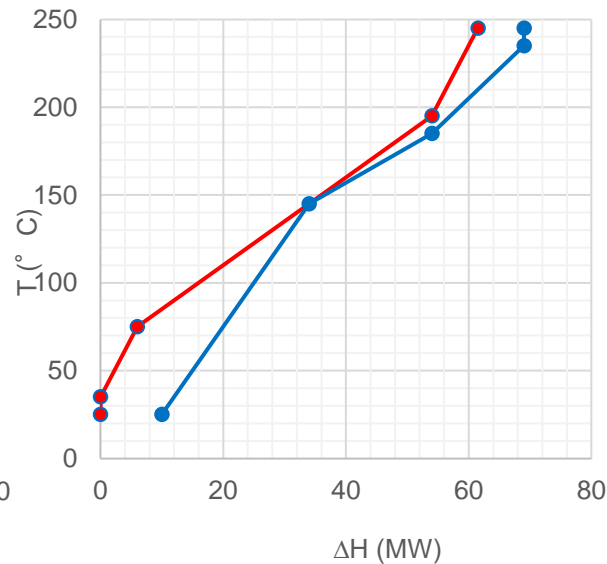
Construction of the Grand Composite Curve (GCC)

Composite curve



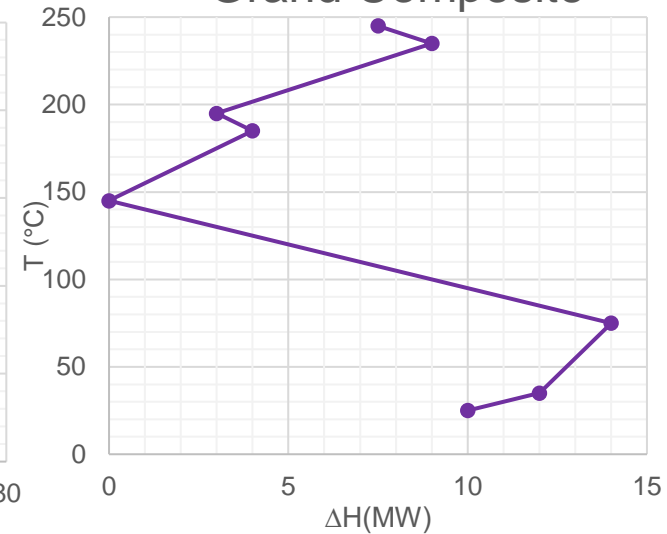
(Courbes composites)

Shifted Composite Curve



(Courbes composites déplacées)

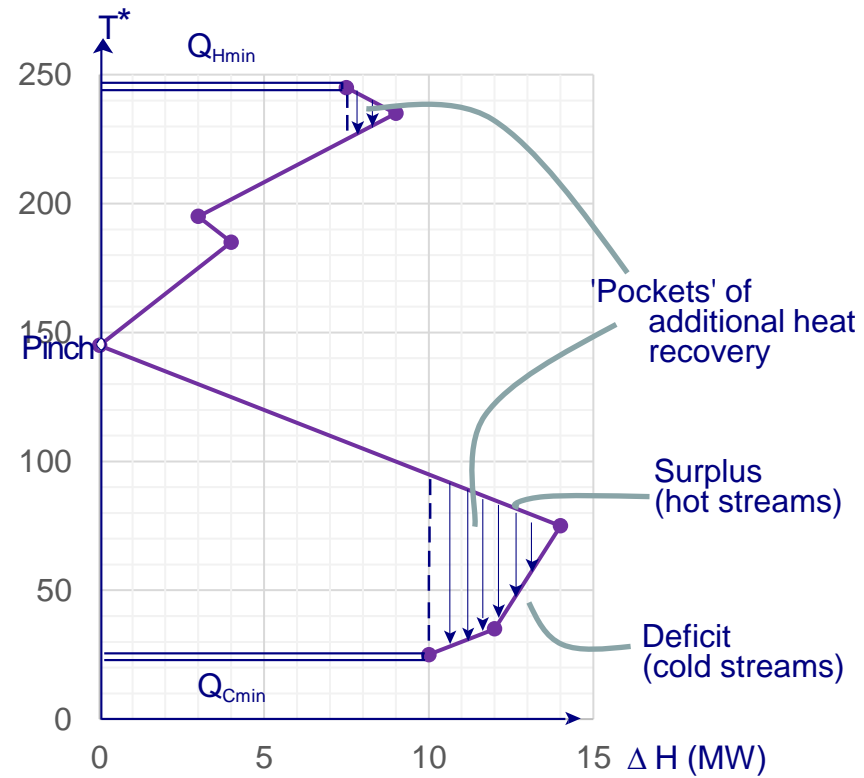
Grand Composite



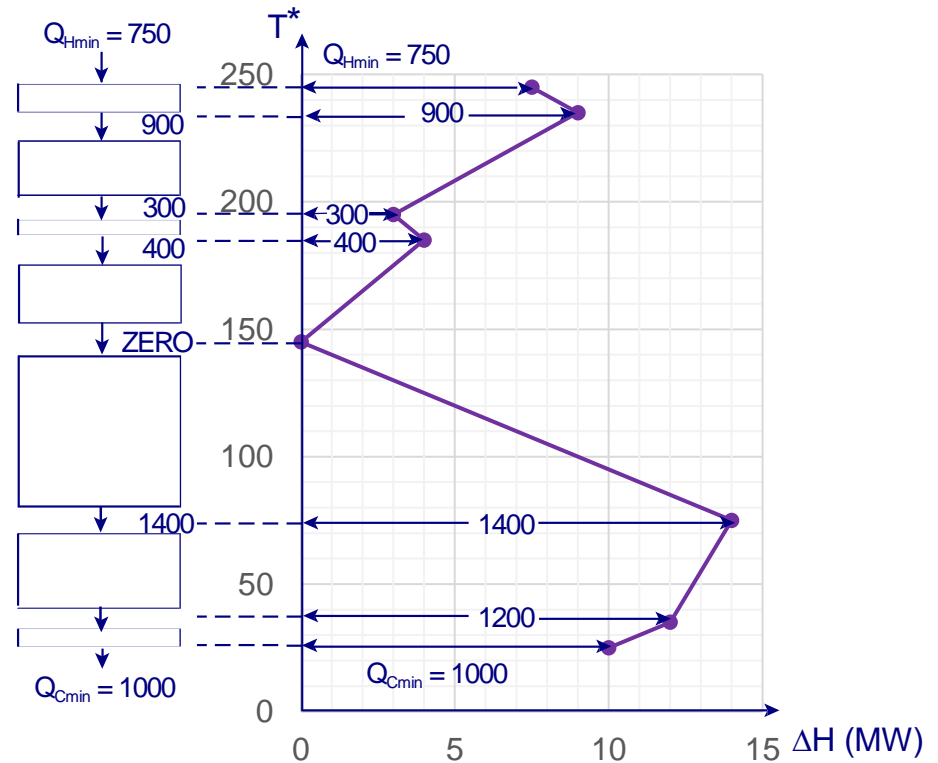
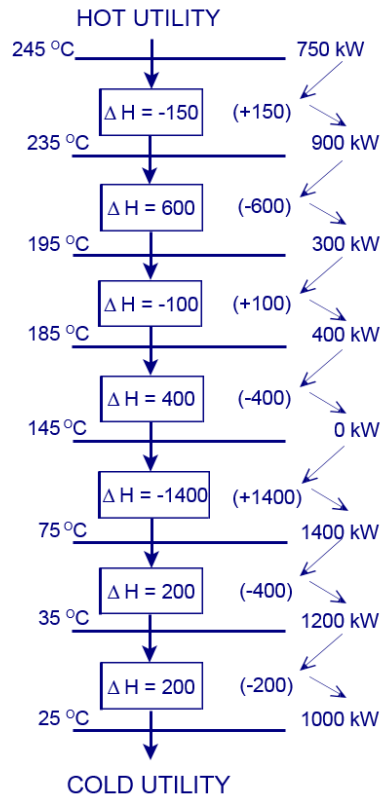
(Courbe grand composite)

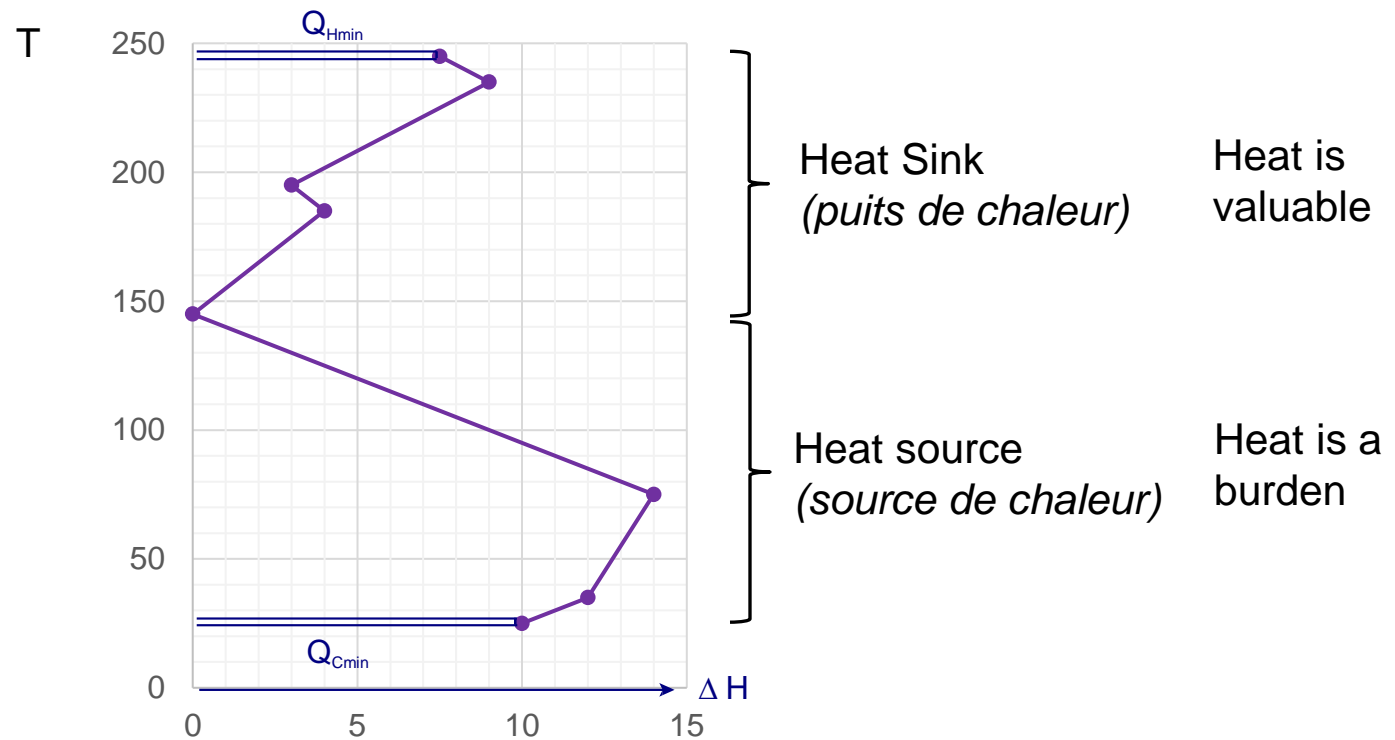
Source: Pinch Analysis:
For the Efficient Use of Energy, Water & Hydrogen. Natural resources Canada. 2003

The “Grand Composite Curve”



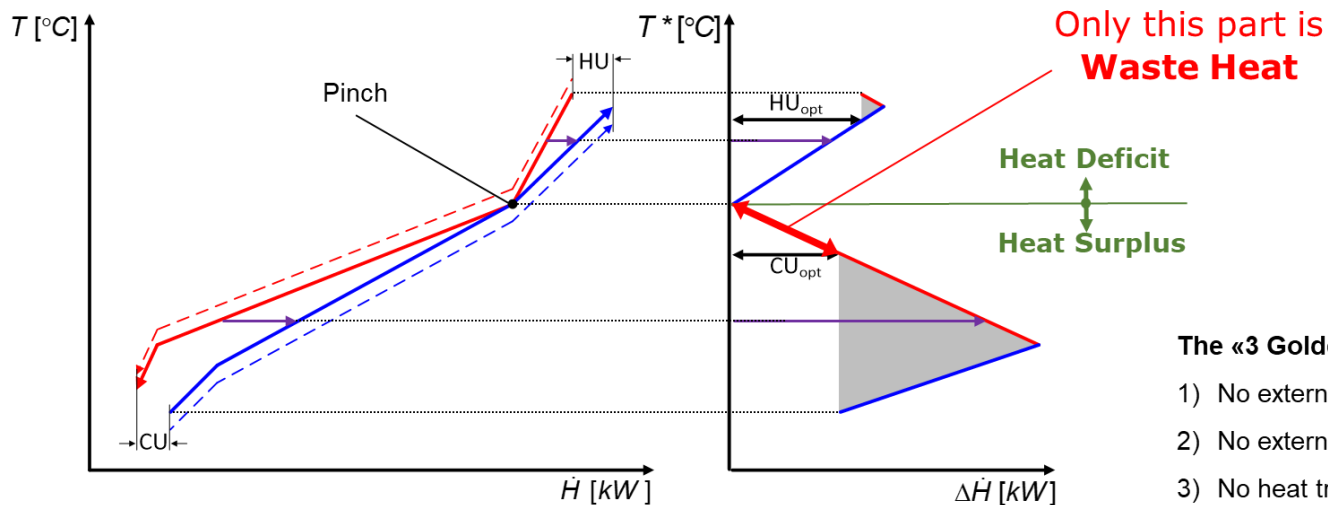
The Problem Table





Grand Composite Curve (GCC)

- Shows the heat deficit and surplus as a function of temperature
- Enables the optimization of the utility supply system (HU_{opt} , CU_{opt})
- **Identifies and characterizes the waste heat** (and excess heat)



The «3 Golden Rules» of Pinch Analysis

- 1) No external cooling above the pinch
- 2) No external heating below the pinch
- 3) No heat transfer over the pinch

Example 2

Stream Data Table

No	Stream	Type	Supply Temp. T_S ($^{\circ}\text{C}$)	Target Temp. T_T ($^{\circ}\text{C}$)	Enthalpy change ΔH (kW)	Heat Capacity Flowrate CP ($\text{kW } ^{\circ}\text{C}^{-1}$)
1	Reactor 1 feed	Cold	20	180	3200	20
2	Reactor 1 product	Hot	250	40	-3150	15
3	Reactor 2 feed	Cold	140	230	2700	30
4	Reactor 2 product	Hot	200	80	-3000	25

CP Table

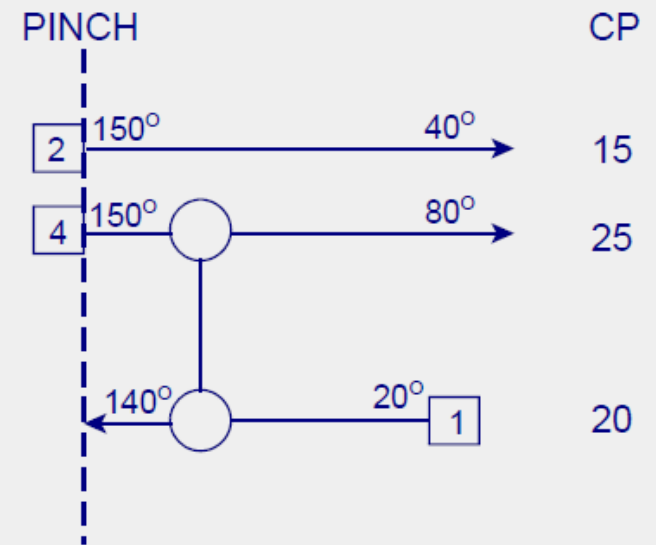
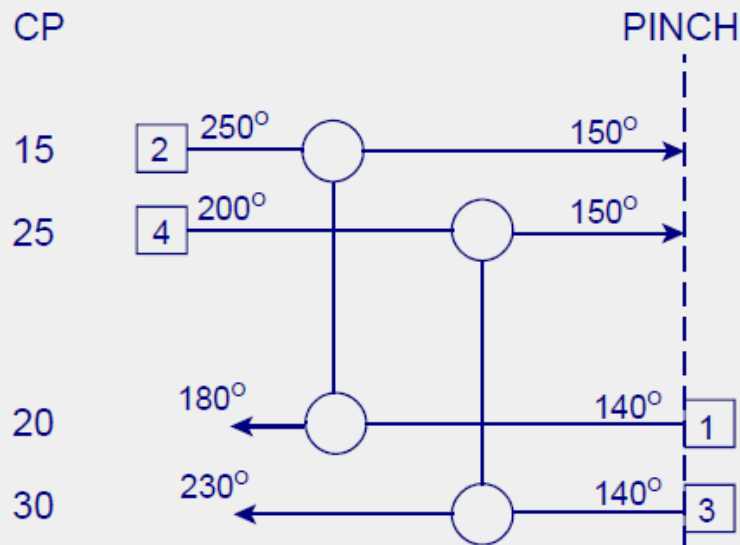
(a) ABOVE PINCH

(b) BELOW PINCH

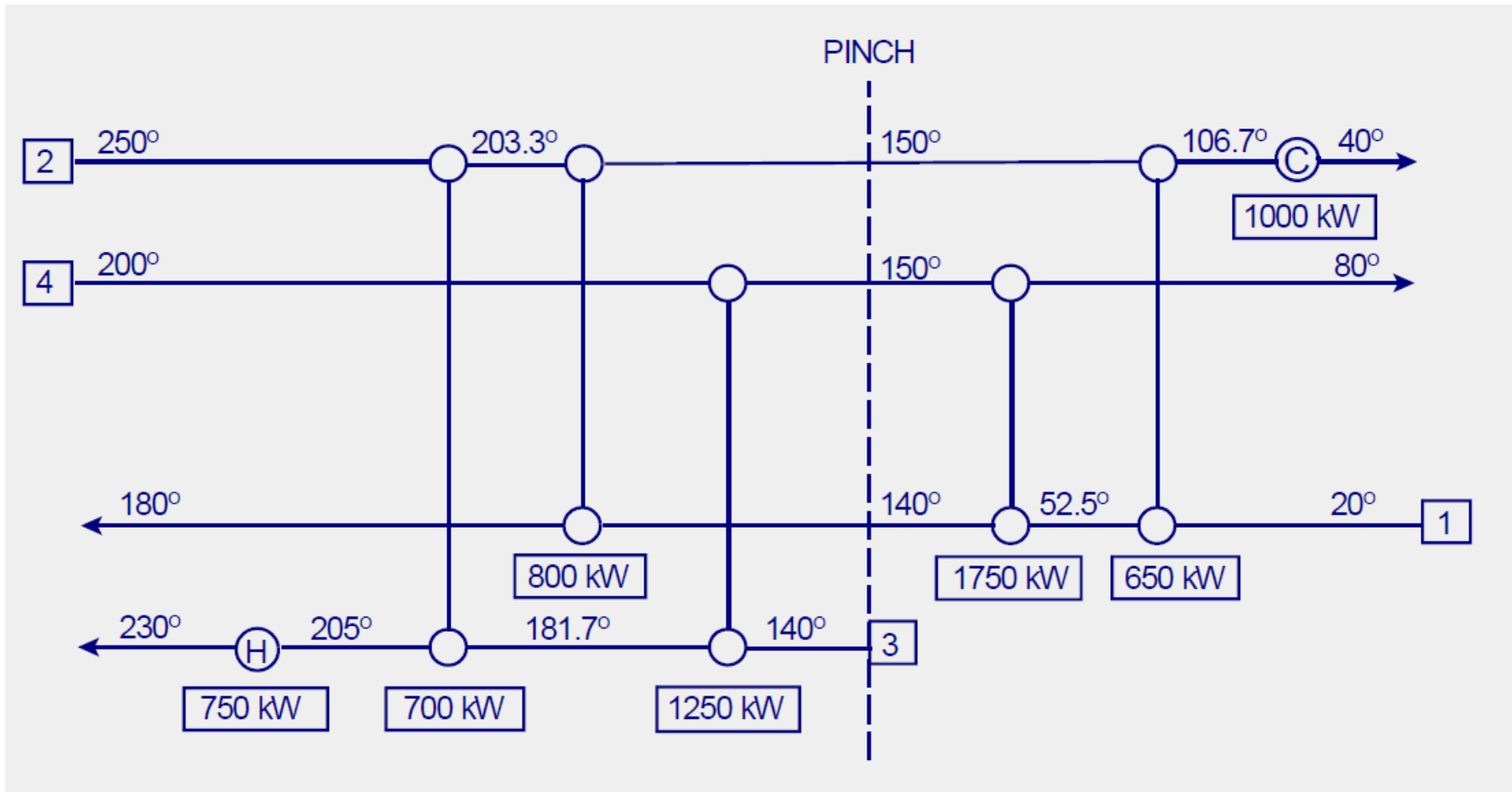
CP's in
descending
order

$CP_H < CP_C$	
25	30
15	20

$CP_H > CP_C$	
25	20
15	



Grid diagram of the Completed Design



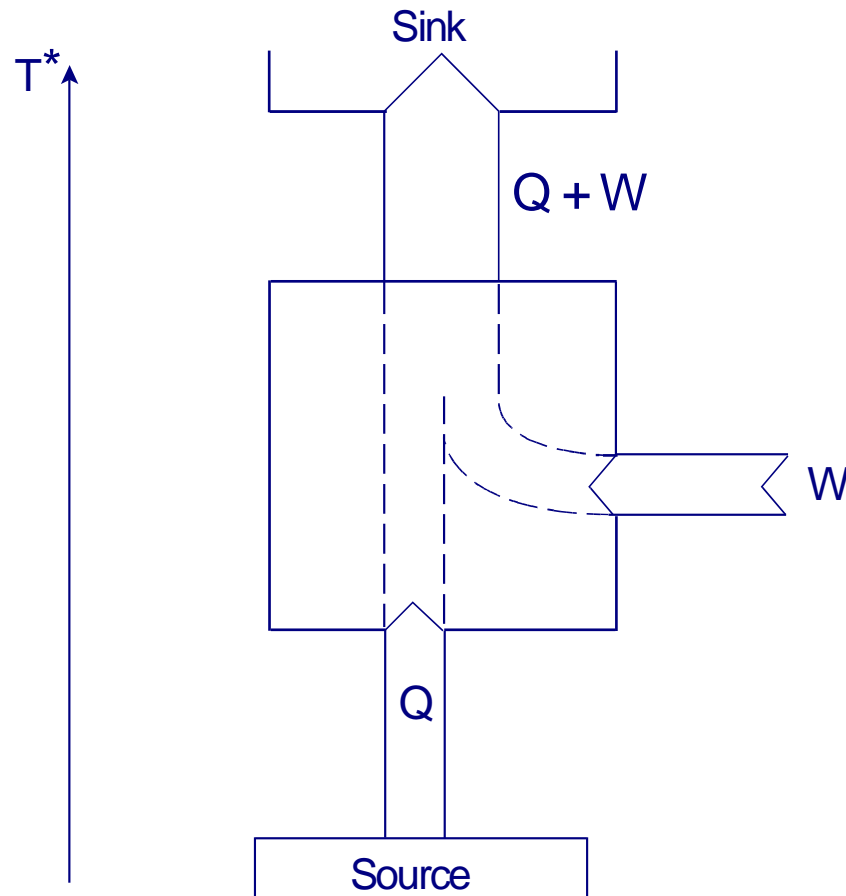
Summary

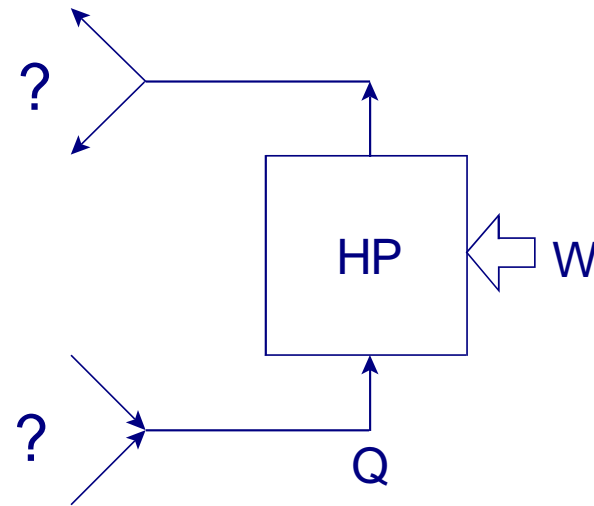
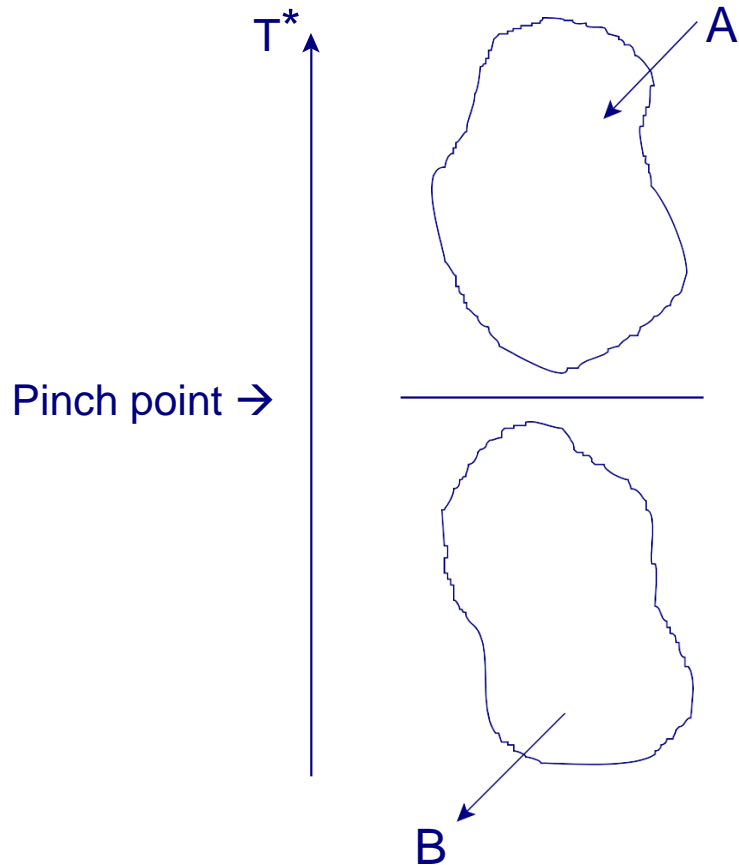
- Composite curve is a graphical approach while problem table algorithm uses a calculation based approach.
- The grid diagram determine the final matching between the heat exchanger and their sizes.

Part 4

Heat Integration of Heat Pumps

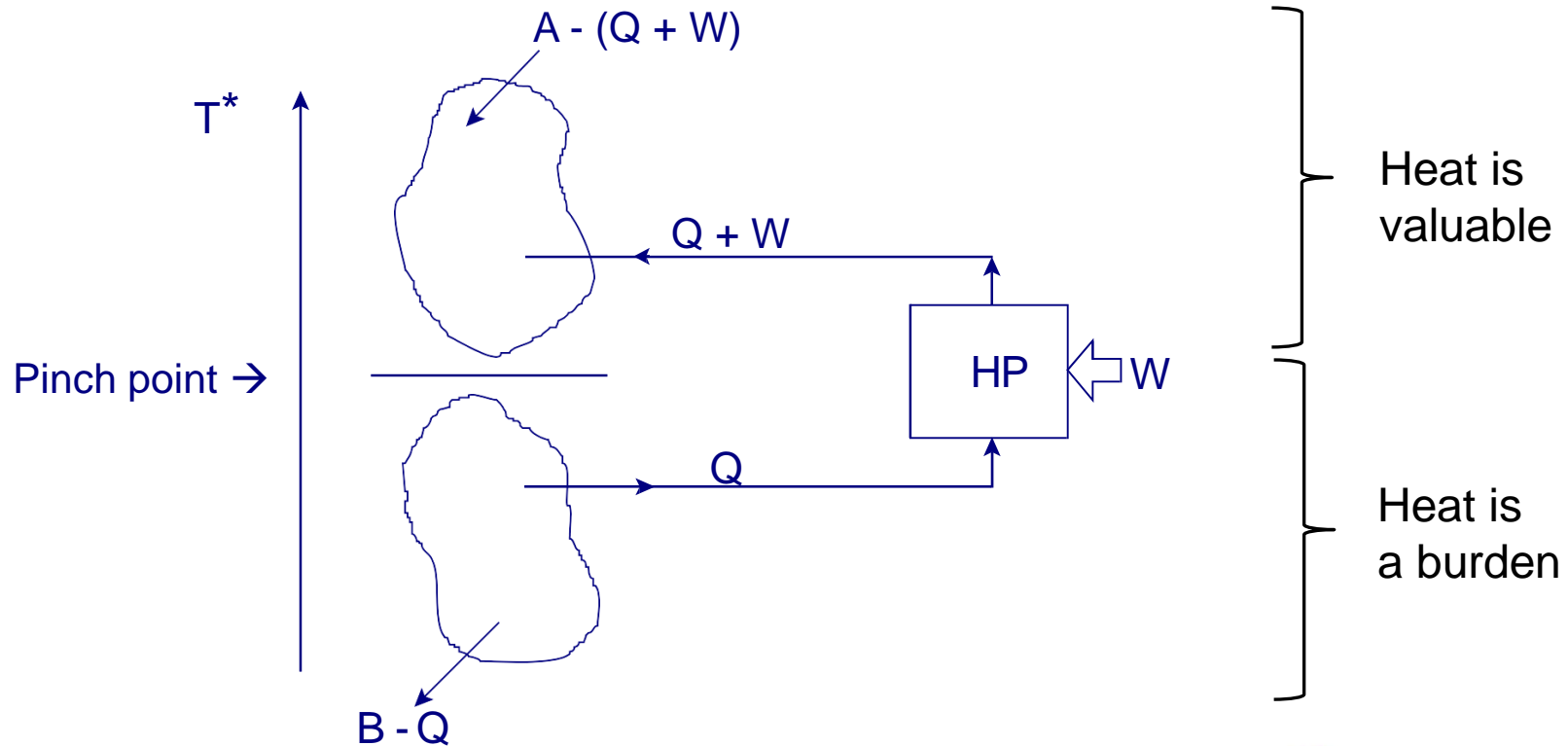
Heat pump (Pompes à chaleur)





How should we integrate a heat pump ?

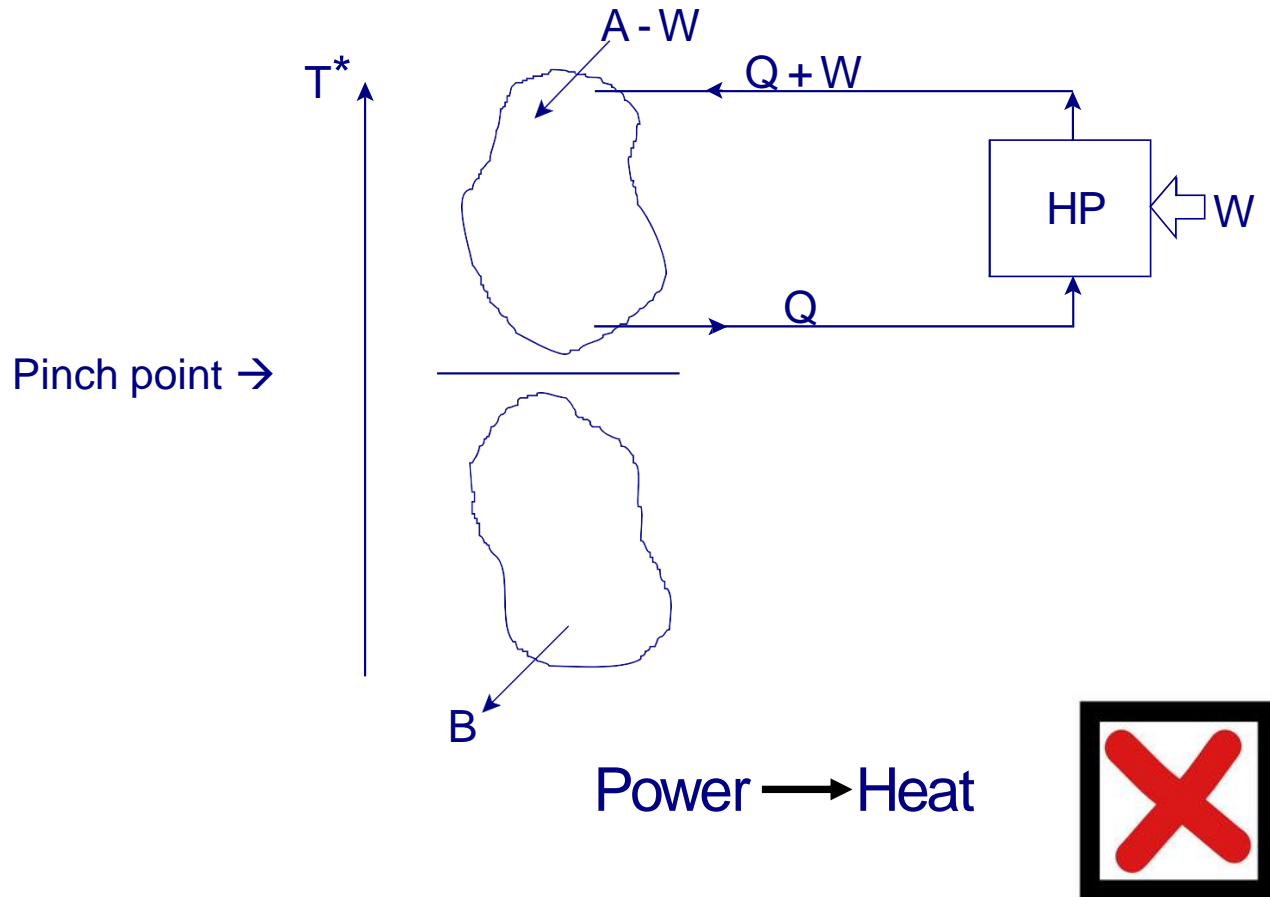
Integrate **HP** across the pinch



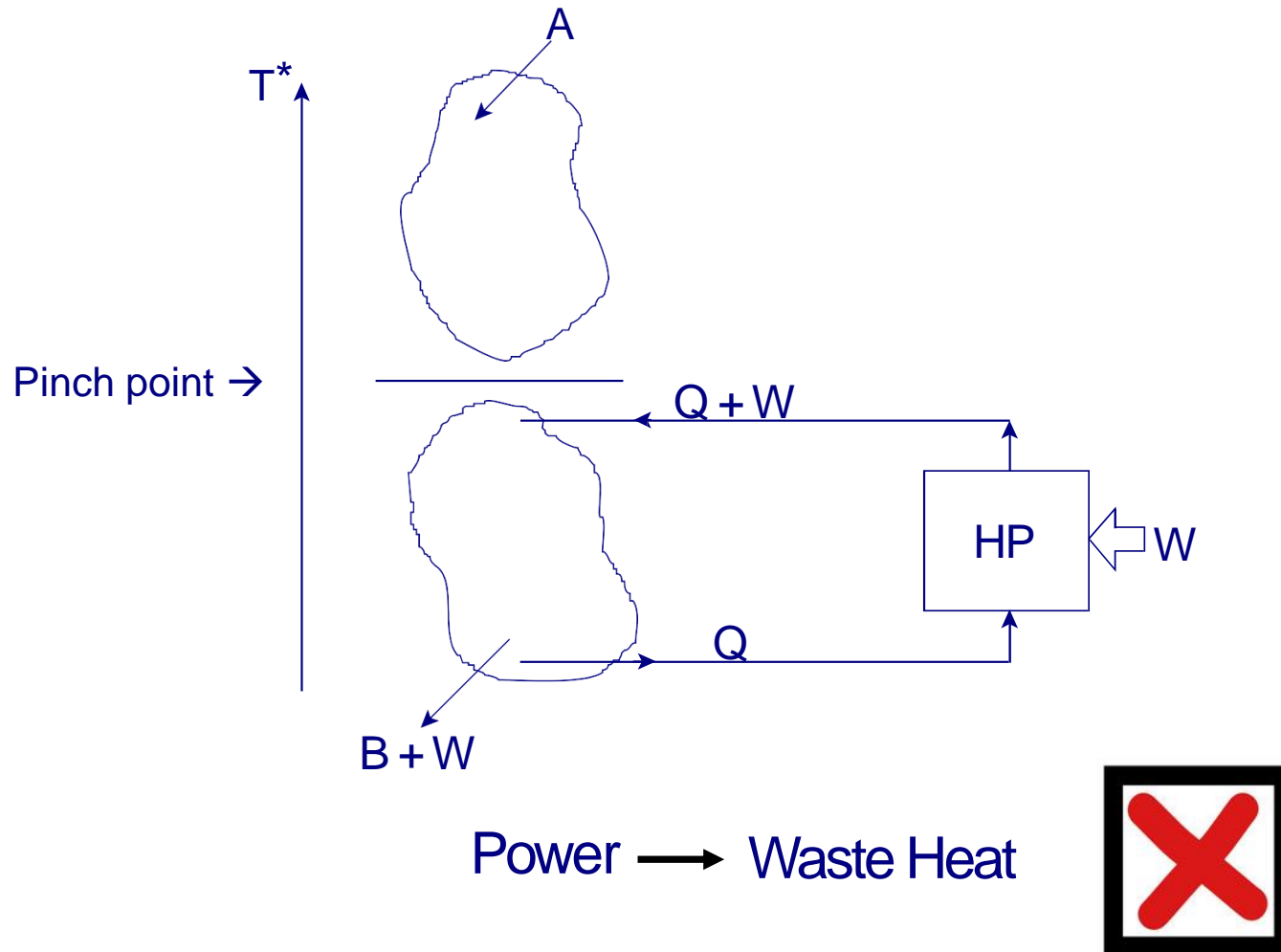
Saves hot and cold utility



Integrate above the pinch



Integrate below the pinch

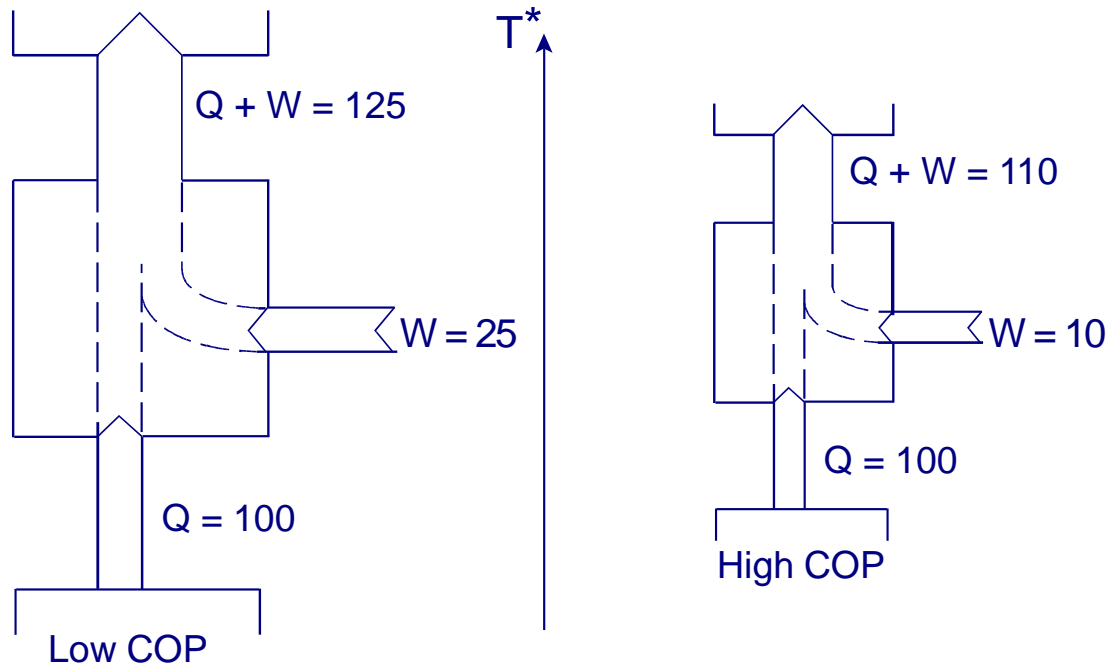


Appropriate Placement of Heat Pumps:

ACROSS THE PINCH

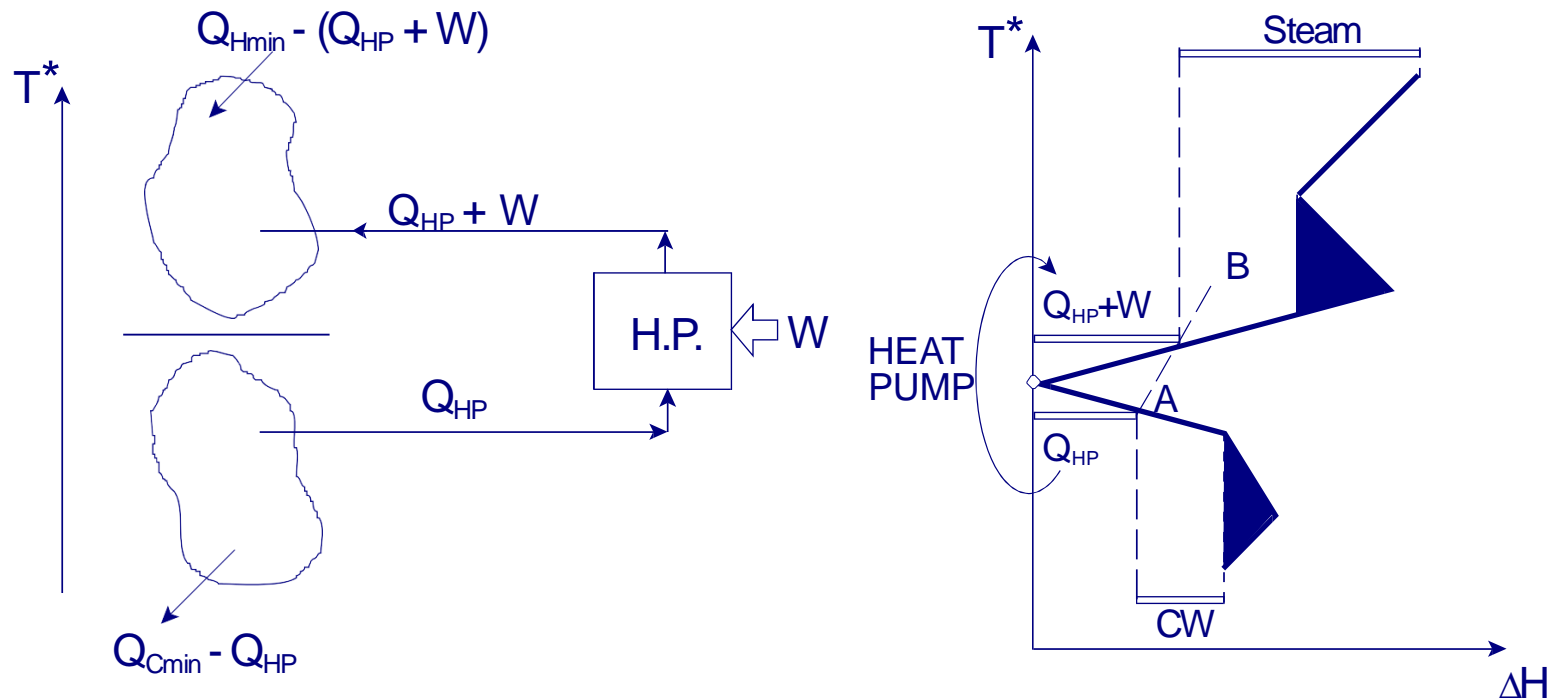
(à travers du point de pincement)

Coefficient of Performance



$$\text{COP} = \frac{Q + W}{W} = f(\Delta T)$$

Try and use Heat Pump across small ΔT s



The grand composite curve allows heat pump cycles to be sized

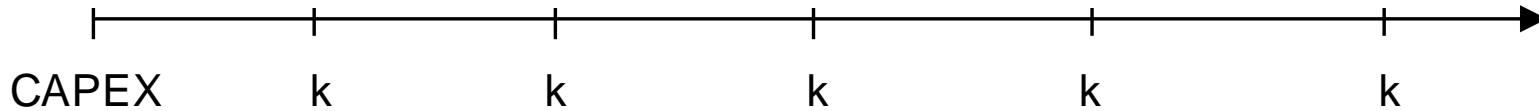
Summary

- Appropriate placement of heat pumps is fundamental
- Match profiles against the grand composite curve

Reminder

Economic assessment

Annuity method (1/2)



$$\text{CAPEX} = \frac{k}{(1+r)} + \frac{k}{(1+r)^2} + \frac{k}{(1+r)^3} + \dots$$

$$\text{CAPEX} = \frac{k}{(1+r)} * \left[1 + \frac{1}{(1+r)} + \frac{1}{(1+r)^2} + \dots \right]$$

$$\text{CAPEX} = \frac{k}{(1+r)} * \left[1 + q + q^2 + \dots \right]$$

$$\text{CAPEX} = \frac{k}{(1+r)} * \left[\frac{q^n - 1}{q - 1} \right]$$

$$\text{CAPEX} = k * \frac{(1+r)^n - 1}{(1+r)^n * r}$$

1/α

k: yearly investment cost
 CAPEX: Capital expenditure
 α: Annuity factor
 r: Interest rate
 L: Lifetime or period of depreciation

Annuity method (2/2)

Investment costs k (per year)

$$k = \alpha * CAPEX$$
$$\alpha = \frac{r}{1 - (1 + r)^{-n}}$$

r = interest rate (discount rate)

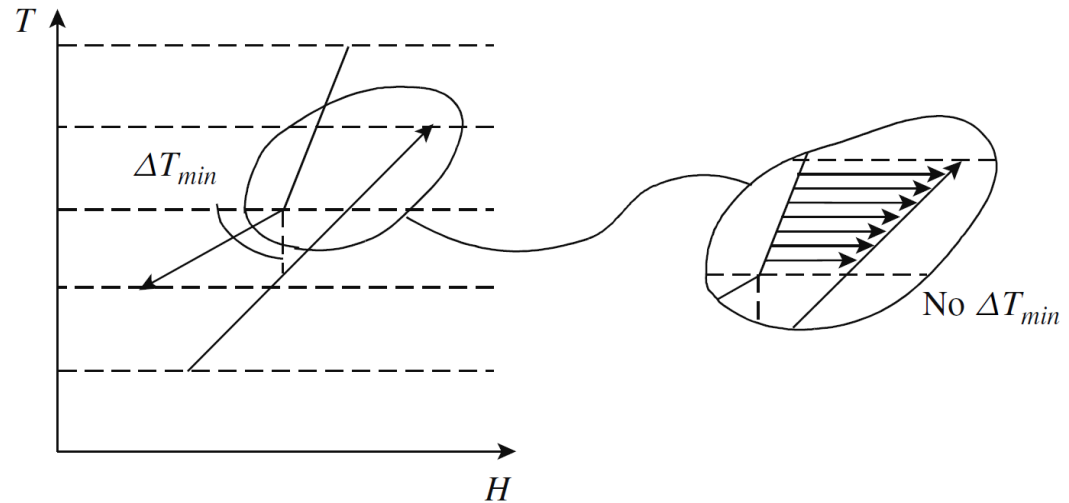
n = (economic) lifetime of the investment
(= period of depreciation)

α = annuity factor



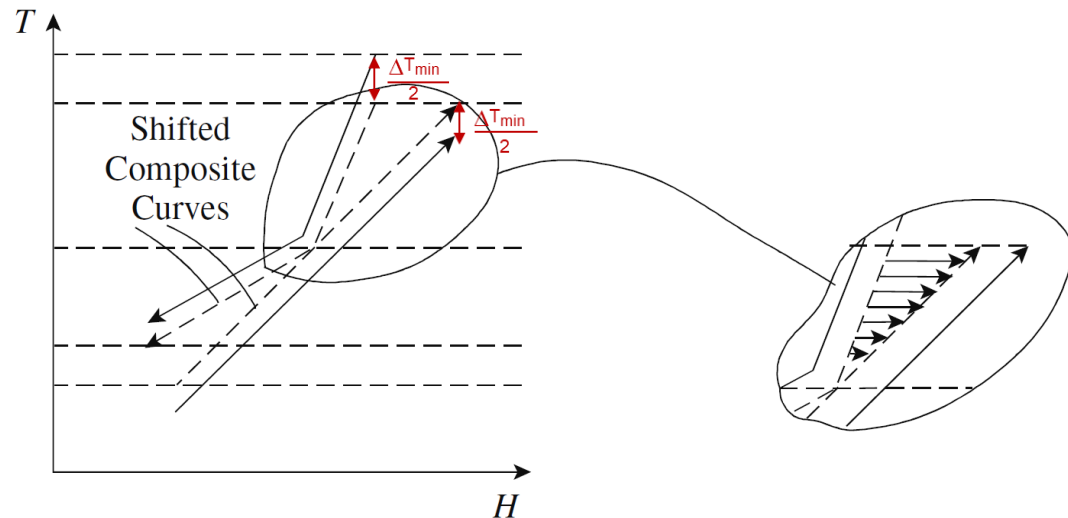
Additional slides

Original Composite Curves



(a) Driving forces not feasible within each interval.

Shifted Composite Curves



(b) Heat transfer within temperature intervals now feasible.

Shift Composite Curves

